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Integration of a Levee Breach Erosion Model in a GPU-Accelerated 2D Shallow Water Equations Code

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1	Integration of a Levee Breach Erosion Model in a GPU-accelerated 2D Shallow Water Equations Code
2	water Equations Code
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9	
10	Key Points:
11 12	• The paper presents a 2D SWE model able to simulate the opening of a levee breach due to overtopping, and the subsequent flooding.
13 14	• The physically based erosion model allows predicting the breach evolution in levees made of cohesive or non-cohesive material.
15 16	• The model can be applied to real cases, thanks to the fast execution times guaranteed by the GPU-parallelization of computations.
17	

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18 Abstract

19 This paper presents a two-dimensional (2D) shallow water equations code coupled with a physically-based erosion model, able to predict the opening and evolution of breaches forming in 20 levees built with either cohesive or non-cohesive material. The bottom elevation change is 21 evaluated using an excess shear-stress equation, which accounts for the hydrodynamic conditions 22 23 and for the material characteristics. The proposed model modifies the local topography at runtime wherever the levee is overtopped without having to predefine the position and shape of 24 the breach. The model is implemented in CUDA programming language, so that simulations can 25 be run on Graphics Processing Units (GPU), guaranteeing fast execution times even for high-26 resolution meshes and large domains. The validation is performed based on several experimental 27 tests, and numerical predictions are in good agreement with the measurements. The strengths and 28 weaknesses of the proposed approach are also discussed by comparison with a sediment 29 transport model based on the Exner equation: while the latter gives good results only for 30 breaches forming in levees built with non-cohesive material, the proposed model can also be 31 applied to cohesive embankments. The application to a historical flood event is also presented, 32 showing that the model can effectively be employed for real field simulations also in the case of 33 multiple breaches. 34

35

36 **1 Introduction**

37 Many lowland areas are protected from flooding by levees, whose main purpose is to confine the 38 flow inside the river region. Levees are usually built with erodible material (clay, silt or sand), and their 39 height is designed to contain a specific hydrograph. However, in the case of an extreme event exceeding 40 their design return period, overtopping occurs, often causing the embankment collapse. Land use 41 modifications and climate change might also increase the discharge for a given return period, making the levees no longer adequate. Moreover, earthen embankments may experience breaching for piping and 42 internal erosion processes, even before the water surface elevation reaches the levee crown. The dens of 43 burrowing animals (e.g. porcupine, badger, nutria) have been recently identified as another cause for 44 levee collapse in Northern Italy (Orlandini et al., 2015; Sofia et al., 2017; Viero et al., 2013). 45 Since embankment failures can have damaging consequences and lead to huge economic and 46 human losses, the design of flood hazard maps and emergency plans is particularly important, and 47 48 numerical modeling represents a powerful tool for these analyses. The simplest approach to model the 49 flood propagation caused by a levee breach is to adopt a one-dimensional (1D) model for the channel, and a two-dimensional (2D) model for the floodable area outside the river region (e.g. Masoero et al., 2013; 50 Vorogushyn et al., 2010). The breaches are included in the 1D model as lateral spillway structures 51 (Mazzoleni et al., 2014), and the outflow from these structures is imposed as upstream boundary 52 53 condition to the 2D model, often neglecting possible backwater effects caused by the presence of road or railway embankments in the floodable region. Moreover, the 1D model cannot accurately describe the 54 markedly 2D flow near the breach inside the river. On the contrary, when both the river and the floodable 55

area are simulated using fully 2D Shallow Water Equations (SWE) models (e.g. Teng et al., 2017), these

57 features can inherently be taken into account. In the past, the choice of using 1D-2D models was often

necessary to reduce the computational effort, but the same outcome can now be achieved by using

59 modern High Performance Computing clusters and/or adopting parallelization techniques, such as

60 implementing codes able to run on Graphics Processing Units (GPUs) (Dazzi et al., 2018; Vacondio et al.,

61 2014, 2017).

The breach opening must be somehow included in the 2D modeling. The detailed simulation of 62 the breach process is actually rather difficult, due to its 3D nature and to the complex interactions between 63 hydrodynamic conditions, bank stability, sediment transport and infiltration processes; however, for 64 practical use in the field of flood simulation, simplified approaches are often introduced. The gradual 65 breach opening can be modelled by a time-varying topography with predefined geometric characteristics 66 (e.g. Dewals et al., 2011), or by coupling the SWE with a 2D sediment transport model (e.g. Faeh, 2007). 67 For example, Vacondio et al. (2016) recently simulated a breach-generated flood with a GPU-68 69 accelerated fully 2D model, adopting a purely geometric approach to describe the breach evolution

70 (specifying the breach position and assuming a trapezoidal shape, with final width and failure time

defined a priori). In this way, however, the levee material characteristics are completely neglected from

the breach modeling, possibly resulting in inaccurate predictions. The hydrodynamic conditions, such as

the upstream inflow in the river, the presence of river bends and floodplains, possible backwater effects

that reduce the velocity of outflowing water (and consequently the erosion), can also severely affect the

breach evolution (Viero et al., 2013). Moreover, for (lateral) fluvial breaches the choice of "geometric"

parameters cannot be assisted by results provided by the parametric (e.g. Froehlich, 2008; Xu & Zhang,

2009) or simplified (e.g. Chen & Anderson, 1987; Fread, 1988; Macchione, 2008; Mohamed et al., 2002;

Visser, 1999; Wu, 2013) models available in the literature (ASCE/EWRI, 2011), which were developed

for (frontal) dam breach configurations. In fact, recent experimental investigations (Elalfy et al., 2017;

80 Kakinuma & Shimizu, 2014; Michelazzo et al., 2018; Rifai et al., 2017; Wei et al., 2016) show that, apart

81 from the very first stages, the evolution of a lateral breach is guite different from what observed in the

82 frontal configuration, due to the different direction of the flow (parallel/tilted vs perpendicular to the levee

83 crest).

The best option for simulating riverine levee breaches would be the use of detailed physicallybased multi-dimensional models, based on the integration of hydrodynamic and morphodynamic equations (e.g. Canelas et al., 2013; Li & Duffy, 2011; Murillo & Garcia-Navarro, 2010). In this way, the flow along the river, through the breach and in the inundated region can be simulated simultaneously without the need of introducing internal boundary conditions at the breach location. Attempts of applying 2D sediment transport models to simulate breaches in dams built with non-cohesive material include Cao

90 et al. (2011), Evangelista (2015), Guan et al. (2014), Juez et al. (2014), Van Emelen et al. (2015), Volz et 91 al. (2012), Wang & Bowles (2006), and Wu et al. (2012), while Faeh (2007) performed a fluvial breach 92 test. Nevertheless, applications to real cases are limited by the heterogeneity and scarcity of data on levee 93 materials, and by the prohibitive computational time required for running these models (unless 94 parallelization techniques are introduces, see Juez et al., 2016). Moreover, the application of these models to breach erosion may be questionable, since most sediment transport equations were derived in uniform 95 flow conditions, for small slopes, and with non-cohesive materials, while the breach development is 96 highly unsteady and often involves high slopes and cohesive sediments. For this reason, Morris et al. 97 98 (2009) suggested that the employment of erosion laws would be more consistent with the breach process. Erosion laws have been applied to dam breach modeling by Chen & Anderson (1987), Morris et al. 99 (2009), and Wang & Bowles (2006), and have the advantage of including specific erodibility parameters 100 in the computations, and of being applicable also to cohesive embankments. In fact, the erosion process of 101 dams/levees built with non-cohesive and cohesive material is quite different (e.g. Morris et al., 2007). In 102 103 the latter case, headcut erosion is observed: one or more rills develop into a series of overfalls, which form a headcut (i.e. a vertical or nearly vertical drop on the bed); the headcut migrates upstream and 104 reduces the dam crest height; this phase is then followed by a breach widening stage. Clearly, this 3D 105 106 process cannot be adequately simulated using a 2D depth-averaged model and sediment transport 107 equations, hence a headcut migration rate is often introduced to model this type of breaches (e.g. Hanson 108 et al., 2005; Wu, 2013). However, since this quantity depends on the same erodibility coefficients that 109 appear in simple erosion laws, such laws can arguably be used to model the general breach process, at least as regards the failure time and the final width, avoiding a detailed description of the headcut 110 111 migration process.

The present work aims at introducing an efficient numerical tool for the simulation of inundations 112 113 generated by levee breaches, including a physically-based prediction of the breach evolution (instead of a geometric approach) and avoiding the necessity of defining its characteristics a priori. The GPU-114 115 accelerated 2D SWE numerical code PARFLOOD (Vacondio et al., 2014, 2017) was coupled with an erosion model, in which an excess shear-stress law is employed to predict the time evolution of the 116 bottom elevation at the levee breach site as a function of the local hydrodynamic conditions and of the 117 material characteristics. The model can be used for either non-cohesive or cohesive embankments. For 118 119 comparison purposes, a simple but robust bedload transport model (Juez et al., 2014) was implemented as well. Both models are enriched by a bank failure algorithm, which simulates the sudden failure of blocks 120 of material due to slope instability. Validation is performed based on four experimental tests, and an 121 122 example of application to the real levee-breach event occurred on the Enza River (Italy) in December 123 2017 is also presented.

124 The paper is structured as follows. Section 2 presents the main features of the proposed model.

125 Section 3 is dedicated to the description of all the test cases used for the validation and application of the

126 model, while in Section 4 a discussion on the advantages and disadvantages of the model is presented. In

127 the last Section, conclusions are drawn.

128

129 **2 Model description**

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The proposed model couples three modules: a hydrodynamic model (already presented in
previous works, see Vacondio et al., 2014, 2017), and two newly developed models for erosion and bank
failure simulations. Moreover, a sediment transport model was implemented for comparison purposes (see
Appendix A).

134 2.1 Hydrodynamic model

The hydrodynamic model (Vacondio et al., 2014, 2017) is based on the 2D SWEs written in integral form (Toro, 2001) as follows:

137
$$\frac{\partial}{\partial t} \int_{A} \mathbf{U} \, \mathrm{d}A + \int_{C} \mathbf{H} \cdot \mathbf{n} \, \mathrm{d}C = \int_{A} (\mathbf{S}_{0} + \mathbf{S}_{f}) \, \mathrm{d}A, \tag{1}$$

138 where A and C are the integration volume area and boundary, respectively, **U** is the vector of conserved

139 variables, $\mathbf{H} = (\mathbf{F}, \mathbf{G})$ is the tensor of fluxes in the *x*- and *y*-directions, **n** is the outward unit vector normal

140 to C, S_0 and S_f are the bed and friction slope source terms, respectively, and t is the time. The well-

141 balanced form of the SWEs, proposed by Liang & Marche (2009), is adopted:

142
$$\mathbf{U} = \begin{bmatrix} \eta \\ uh \\ vh \end{bmatrix}, \quad \mathbf{F} = \begin{bmatrix} uh \\ u^2h + \frac{1}{2}g(\eta^2 - 2\eta z) \\ uvh \end{bmatrix}, \quad \mathbf{G} = \begin{bmatrix} vh \\ uvh \\ v^2h + \frac{1}{2}g(\eta^2 - 2\eta z) \end{bmatrix}, \quad (2a)$$
143
$$\mathbf{S}_0 = \begin{bmatrix} 0 \\ -g\eta \frac{\partial z}{\partial x} \\ -g\eta \frac{\partial z}{\partial y} \end{bmatrix}, \quad \mathbf{S}_f = \begin{bmatrix} 0 \\ -gh \frac{n_f^2 u \sqrt{u^2 + v^2}}{h^{4/3}} \\ -gh \frac{n_f^2 v \sqrt{u^2 + v^2}}{h^{4/3}} \end{bmatrix}, \quad (2b)$$

In Eq. (2), $\eta = h + z$ is the water surface elevation, *h* is the flow depth, and *z* is the bed elevation; *u* and *v* are the velocity components along the *x*- and *y*-directions respectively, n_f is Manning's roughness coefficient, and *g* is the acceleration due to gravity.

An explicit FV scheme is used to discretize the equations; both first-order and second-order
 accurate approximations in space and time are implemented, but only the first-order approximation is here
 recalled for the sake of brevity. The following equation is used to update the conserved variables in time:

150
$$\mathbf{U}_{i,j}^{n+1} = \mathbf{U}_{i,j}^{n} - \frac{\Delta t}{\Delta x} \left(\mathbf{F}_{i+\frac{1}{2},j} - \mathbf{F}_{i-\frac{1}{2},j} \right) - \frac{\Delta t}{\Delta y} \left(\mathbf{G}_{i,j+\frac{1}{2}} - \mathbf{G}_{i,j-\frac{1}{2}} \right) + \Delta t \left(\mathbf{S}_{0} + \mathbf{S}_{f} \right).$$
(3)

151 Subscripts *i*, *j* represent the cell position, while superscript *n* refers to the time level; Δx and Δy are the cell

- 152 dimensions in the x and y directions respectively, and Δt is the time step size. The HLLC approximate
- 153 Riemann solver (Toro, 2001) is used to compute intercell fluxes, and the correction proposed by
- 154 Kurganov & Petrova (2007) is implemented to avoid non-physical velocity values at wet/dry fronts. The
- 155 slope source term is discretized with a centered approximation (Vacondio et al., 2014), while the friction
- source term is discretized using the implicit formulation proposed by Caleffi et al. (2003). The minimum
- allowable time step is computed according to the CFL stability condition (Toro, 2001). The model is
- implemented in a CUDA/C++ code, which exploits the intrinsic parallelization of computations on GPU
- 159 devices, thus guaranteeing fast execution times compared to serial codes. More details on the scheme and
- 160 implementation can be found in Vacondio et al. (2014, 2017).
- 161 2.2 Erosion model

The breach evolution is predicted according to the erosion model described in the following. The bottom elevation change is not allowed in the whole domain, but only along the erodible levees, where potential breaches might occur. In these selected regions, the morphodynamic evolution is described by the following equation:

166
$$\frac{\partial z}{\partial t} = -\frac{E}{1-p},\tag{4}$$

where p is the bed porosity, and E is the bed erosion rate (eroded volume per unit area per unit time). This latter quantity can be estimated according to a linear erosion law, also referred to as excess stress equation (e.g. Hanson & Simon, 2001; Partheniades, 1971):

170
$$E = \begin{cases} k_d(\tau - \tau_c) & \text{if } \tau > \tau_c \\ 0 & \text{if } \tau \le \tau_c \end{cases}$$
(5)

In Eq. (5), k_d represents the erodibility coefficient of the embankment material, while τ and τ_c are the bed shear stress and its critical value for sediment motion, respectively. The bed shear stress is computed as follows:

175 where γ is the specific weight of water. Eq. (4) is simply discretized as follows:

176
$$z_{i,j}^{n+1} = z_{i,j}^n - \frac{E(\tau_{i,j})}{1-p} \Delta t.$$
 (7)

In essence, Eq. (7) modifies the bottom elevation of each cell (belonging to an erodible levee) at runtime according to the local value of the bed shear stress, and non-negligible erosion is only obtained in the practice whenever and wherever the levee is overtopped. The opening of a breach, and its subsequent deepening and widening, is then predicted automatically, without the need to predefine the breach position and dimensions as input data. A minimum bed elevation can also be specified in order to avoid erosion below a non-erodible foundation. From Eq. (7), it can be noticed that only scour is allowed, while
deposition of sediments is not included in the computations: the eroded material is supposed to be washed

- away by the flow, in line with other simplified approaches. Conversely, the global water volume is
- 185 conserved by maintaining the original water depth of each cell where sediment is eroded; hence, the water
- 186 surface elevation must be adjusted in these cells by subtracting the scour computed during the current
- 187 update.

By means of Eqs. (4) and (5), the breach erosion process depends both on the flow field 188 characteristics (via τ) and on the embankment material (via k_d , τ_c , and p). The erodibility parameters k_d 189 190 and τ_c control the erosion process, and thus must be accurately calibrated. Despite the fact that specific experimental tests for their determination were developed, such as the Jet Erosion Test (JET) (Hanson & 191 Cook, 2004), reliable correlations with the sediment characteristics are not available yet. Different test 192 configurations and interpretations of results lead to different estimates for k_d and τ_c (Khanal et al., 2016), 193 and even the use of a linear erosion law is still debated (Walder, 2015). Moreover, these parameters are 194 195 observed to be quite sensitive not only to the type of material, in particular to soil texture and plasticity, but also to the compaction effort and water content (Fell et al., 2013; Nguyen et al., 2017; Wahl et al., 196 197 2009), with a variability up to 2-3 orders of magnitude (Hanson & Hunt, 2007). Therefore, the choice of 198 erodibility parameters must be carefully considered, and the uncertainty in their values must be properly 199 taken into account by means of a sensitivity analysis when data for calibration are not available. The 200 diagram and tables reported by Hanson et al. (2010) can provide guidance for defining the range of 201 variability of these parameters. Moreover, some authors suggest empirical relationships between τ_c and k_d (e.g. Hanson & Simon, 2001; Nguyen et al., 2017); Wu (2013) also reports an empirical formula for 202 computing the erodibility coefficient (based on the clay content and the dry specific weight of the soil), 203 204 which can help in the choice of reasonable values when specific erosion tests cannot be performed.

205 2.3 Bank failure algorithm

While the breach triggering is mainly due to the erosion following levee overtopping, its 206 207 enlargement is also due to the sudden collapse of the lateral banks, which lose stability as long as the 208 breach deepens (Hunt et al., 2005). Numerical models must consider this mechanism for a correct 209 prediction of the breach development. For this reason, different bank failure algorithms were presented in 210 the literature (e.g. Evangelista et al., 2015; Swartenbroekx et al., 2010; Volz et al., 2012), usually based on the idea of reducing the local slope of each cell when it exceeds a critical value φ_c . Obviously, all these 211 models ignore cantilever failures, which are sometimes observed in experimental tests (e.g. Wei et al., 212 2016), but cannot be described in a depth-averaged model. In this work, the scheme of Guan et al. (2014) 213 for structured grids was adapted for guaranteeing efficiency on GPUs. 214

215 Two different values are specified for the critical angles, depending on the fact that the cell is 216 above or below the water surface level: $\varphi_{c,wet}$ for wet cells, and $\varphi_{c,dry}$ for dry cells; moreover, φ_{dep} is the angle that the deposited material forms after collapse. These values are often assumed equal to the 217 angle of repose of the material. Let us consider cell (i,j) with bottom elevation $z_{i,j}$ in a Cartesian grid, 218 with four neighbor cells (i+1,j), (i-1,j), (i,j+1), (i,j-1). The local slope φ_k in the k^{th} direction can be 219 computed as: 220 $\tan \varphi_k = (z_k - z_{i,i})/l_k,$ (8) 221 where z_k is the bottom elevation of the neighboring cell in the k^{th} direction (i.e. cell (i+1,j) to the east, cell 222 (i,j+1) to the north, etc.), and l_k is the grid size in the same direction (i.e. Δx to the east/west, and Δy to 223 the south/north). If $|\varphi_k| > \varphi_c$ (wet or dry, depending on the cell state), then the bottom is considered 224 225 locally unstable, and a correction Δz_k can be calculated as:

226
$$\Delta z_k = 0.5 l_k \left(\tan |\varphi_k| - \tan \varphi_{dep} \right) \operatorname{sign}(\varphi_k).$$
(9)

An equal and opposite correction will be computed in the neighboring cell, so that the total sediment mass is conserved in this procedure, and the bed slope is simply tilted from φ_k to φ_{dep} . Finally, the updated value for the bottom elevation becomes:

230
$$z_{i,j}^{new} = z_{i,j} + \sum_{k=1}^{4} \Delta z_k.$$
 (10)

These operations are performed in a specific CUDA kernel, and threads (i.e. the basic work unit in CUDA, corresponding to one computational cell) are processed in parallel. Differently from Guan et al. (2014), that processed all cells sequentially, and applied the correction Δz_k both to the current cell and to its neighbor (with proper sign), in this implementation each thread computes its own corrections, even at the cost of repeating calculations twice in two different threads. As already discussed in Vacondio et al. (2014) as regards intercell fluxes, accepting this small computational overhead makes the code more efficient than storing an extra array for the values of Δz_k and accessing it later.

238 Obviously, local changes in the bed slope may in turn affect the stability of other neighboring 239 cells. The algorithm previously described, then, must be repeated iteratively until no more corrections are 240 necessary. In order to reduce the computational time, this recursive procedure is not performed at every 241 time step Δt dictated by the CFL condition, but at a larger pace Δt_{stab} ; in particular, preliminary tests 242 showed that checking and correcting the slope stability with Δt_{stab} =500-1000 Δt provides the same results 243 as with Δt_{stab} = Δt .

244

245 **3 Numerical tests**

In this Section, five test cases are presented for the validation of the erosion model. The first case 246 is a 1D frontal dam breach experiment, and was chosen for its simplicity in order to highlight the 247 differences in the predictions of the erosion model compared to a sediment transport model. Moreover, 248 two 2D frontal breach test cases, which differ in the type of material used for building the dam (cohesive 249 vs. non-cohesive), were considered in order to assess the capability of predicting the breach enlargement, 250 251 and to study the influence of the model parameters on the simulation results. Then, since the erosion model is conceived for real field applications to fluvial breaches, a large-scale experimental test case 252 concerning a lateral breach in a channel was privileged over available small-scale laboratory experiments 253 as the fourth validation test, and it still involves levees built with non-cohesive material. Finally, the 254 applicability of the model to a real event is assessed by means of the simulation of the levee breach on the 255 Enza River (Northern Italy) and the subsequent flooding occurred in December 2017. 256

257 3.1 1D frontal dam breach

The experimental test concerning dam erosion due to overtopping, reported by Tingsanchali & 258 259 Chinnarasri (2001) (Test C-2), was simulated in order to compare the results of the erosion and the sediment transport models. A 0.8 m-high dam, with crest width equal to 0.3 m and upstream and 260 downstream slopes equal to 1V:3H and 1V:2.5H respectively, was built in a 35 m-long, 1 m-wide 261 rectangular flume. The dam was built with sand with the following characteristics: $d_{50} = 0.86$ mm, $d_{30} =$ 262 0.52 mm, $d_{90} = 3.80$ mm, $d_m = 1.13$ mm, and $\rho_s = 2650$ kg/m³. A constant inflow (1.23 l/s) was supplied at 263 the upstream end of the channel; a vertical plate was held at the dam crest until the reservoir was filled, 264 265 and the water depth in the reservoir was 3 cm higher than the dam crest; then, the sudden removal of the 266 plate allowed overflow to start.

The domain was discretized by means of a uniform grid with $\Delta x = \Delta y = 0.05$ m. The following parameters were common to both erosion and sediment transport models: bed porosity p = 0.4, critical angles $\varphi_{c,wet} = \varphi_{dep} = 30^\circ$, $\varphi_{c,dry} = 50^\circ$. Manning's coefficient and the erosion model parameters, τ_c and k_d , were subjected to calibration, and a sensitivity analysis on their values was performed.

First, Manning's coefficient was determined by simulating the experiment with the sediment transport model, which did not require any other calibration coefficient. Figures 1a-1b compare the experimental dam profiles along the centerline of the breach at selected times (t = 30 s and t = 60 s) and the results from the numerical simulations performed assuming $n_f = 0.016$ m^{-1/3}s, 0.018 m^{-1/3}s, and 0.020 m^{-1/3}s. An increase in this coefficient leads to a slightly more rapid erosion. However, there is no clear best fit value; in the first phases (Fig. 1a), the smallest roughness value seems to mimic the dam erosion better, while it underestimates the erosion at the dam crest after some time (Fig. 1b). The intermediate value $(0.018 \text{ m}^{-1/3}\text{s})$ is hence selected for describing the general process.

The erosion model was tested next. As a starting point for choosing the erodibility parameters, the work by Hanson et al. (2010) was considered: for soils with low clay content, the suggested values for k_d

are in the range 50-800 cm³/N/s (depending on compaction); the corresponding τ_c range is 10^{-3} - 10^{-1} Pa.

Preliminary simulations were performed varying τ_c (10⁻³, 10⁻², and 10⁻¹ Pa) with different values 282 of k_d , and results of these tests show that changes in the values of τ_c have negligible effects in the process, 283 because the bed shear stress exceeds the critical value by 1-2 orders of magnitude ($\tau >> 1$). Then, τ_c was 284 285 assumed equal to 10^{-2} Pa, and the erodibility coefficient was varied: the best fit was obtained for $k_d = 500$ cm³/N/s. In Figures 2a-2b, the simulated and measured dam profiles along the centerline at selected times 286 for different values of k_d (300, 400, 500, and 600 cm³/N/s) are reported, and stress how much the choice 287 of this parameter can influence the breach evolution. The fact that the proposed model can only reproduce 288 the erosion process can be clearly noticed from this comparison: while experimentally the downstream 289 290 slope flattens as long as the dam crest is eroded because sediments are deposited at the dam toe, numerically the downhill slope simply retreats due to erosion; nevertheless, the calibrated value for k_d 291 guarantees that the model predicts the eroded dam crest height correctly. The outflow discharge is 292 reproduced reasonably, and the peak value is well predicted, as can be observed in Figure 2c, even if the 293 294 model, probably due to the differences in the bathymetry towards the end of the simulation (caused by the 295 exclusion of the deposition processes), overestimates the falling limb of the hydrograph. The outflow 296 discharge predicted by the sediment transport model is also reported in Figure 2c for the sake of 297 comparison; the dam erosion is probably too fast in the first stages, and the reservoir emptying is anticipated compared to experimental observations, leading to a lower discharge peak. 298

3.2 2D frontal breaches

In this section, a sensitivity analysis on the erosion model parameters is undertaken by simulating 300 two 2D frontal breaches experimental test cases performed at the HR Wallingford laboratory for the 301 302 IMPACT project (Morris et al., 2005). All tests were carried out in a 50 m long and 10 m wide flume, 303 where an erodible dam was built roughly 36 m downstream from the channel entrance (Figure 3a). Water 304 was allowed into the flume until the reservoir upstream of the dam was filled and the water level 305 exceeded the elevation of a pilot channel carved in the central portion of the dam, thus triggering the breach opening. Tests labelled #2 and #10 were selected, and the main features of these experiments are 306 307 reported in Table 1. Notably, in Test #2 the dam was built with non-cohesive material (nearly uniform sand with $d_{50} = 0.25$ mm), while for Test #10 a cohesive material (clay) was employed; the breach 308 evolution was hence different for the two tests. For the non-cohesive dam, the first phase was similar to 309

- the 1D case, and was characterized by uniform erosion on the downhill slope, which retreated and became
- 311 milder at the dam section corresponding to the pilot channel. On the other hand, for the test with a
- 312 cohesive dam, headcut erosion was observed on the downhill slope. Then, in both cases, the breach side
- slopes started to lose stability and bank failures occurred, so that the breach enlarged in time
- symmetrically; the process ended when the upstream reservoir was almost empty.
- For both tests, the domain was discretized with square cells of size $\Delta x = \Delta y = 0.05$ m, and Manning's coefficient was set equal to 0.018 m^{-1/3}s for Test #2 (as suggested by Wu et al., 2012), and to 0.016 m^{-1/3}s for Test #10 (according to Wu, 2013). The time series for the inflow discharge were imposed as upstream boundary condition, while a free outlet condition was set downstream.
- Test #2 is analyzed first. As in the previous test case, the values of the erodibility parameters were chosen in the range suggested by Hanson et al. (2010) for low clay content soils. In particular, the best fit was obtained with $\tau_c = 10^{-2}$ Pa, and $k_d = 150$ cm³/N/s. The other model parameters were set as follows: $p = 0.4, \varphi_{c,wet} = \varphi_{dep} = 30^{\circ}, \varphi_{c,dry} = 45^{\circ}$. Figures 3b-3e show the bottom elevation contour maps at selected times, together with the velocity vectors. The absence of deposition downstream can be noticed, but the "hourglass" shape in the first phase of the breach opening and the final top width are well reproduced.
- The measured and simulated breach top widths in time are reported in Figure 3f. Results obtained 325 with three different values of the erodibility coefficient are compared ($k_d = 100, 150, \text{ and } 200 \text{ cm}^3/\text{N/s}$, 326 327 while all the other parameters are kept constant). The model with $k_d = 150 \text{ cm}^3/\text{N/s}$ is able to reproduce 328 the breach evolution in time quite well. However, regardless of the selected erodibility coefficient, the 329 model underestimates the outflow discharge, as can be observed in Figure 3g. The model slightly anticipates the beginning of the breach enlargement, which is more rapid in the experiments than in the 330 numerical simulations, and this may influence the outflow discharge and the reservoir emptying process. 331 332 Another possible cause of these discrepancies can be the uncertainty in the position and technique of the discharge measurements (the dam centerline is used as cross-section for the discharge extraction in the 333 334 numerical simulations, while no information is available as regards the experimental setup).
- Additional sensitivity analyses were performed on Manning's coefficient, on the critical shear 335 stress, and on the critical angles for slope stability, which are expected to influence the breach 336 enlargement. The values 0.016 and 0.020 m^{-1/3}s for Manning's coefficient were investigated. The critical 337 shear stress τ_c was varied to 10^{-3} and 10^{-1} Pa, maintaining all the other parameters constant. The critical 338 angle for slope stability in wet conditions $\varphi_{c,wet}$ (and the angle of deposition φ_{dep}) was changed from 30° to 339 25° and to 35°; as regards $\varphi_{c,dry}$, the values 40°, 50°, 60°, 70° were examined. For all these simulations, 340 the main breach characteristics (final top width, peak discharge) are reported in Table 2, and the relative 341 342 error with reference to the experimental measurement and to the best-fit simulation is computed. The 343 critical shear stress has negligible influence on the results, as already noticed in the previous test case.

- 344 Moreover, results are observed not to be much dependent on the "wet" critical angle for slope stability.
- On the other hand, an increase in the value of $\varphi_{c,dry}$ can reduce the final breach width and the peak
- discharge. Finally, Manning's coefficient does not particularly affect the main breach features. In fact,
- 347 despite the fact that τ increases quadratically with n_f (Equation 6), at the same time velocity magnitude
- 348 decreases, thus limiting the variation of the bed shear stress.
- For simulating Test #10, erodibility parameters for a cohesive soil had to be set. Following Hanson et al. (2010), and also considering the formula for the estimation of k_d reported by Wu (2013), the range 0.1-10 cm³/N/s can be considered adequate for the erodibility coefficient value of this kind of material. The critical shear stress τ_c should be set in the range 0.01-1 Pa. The following parameters were selected for the reference simulation: p = 0.4, $\tau_c = 0.1$ Pa, $k_d = 5$ cm³/N/s, $\varphi_{c,wet} = \varphi_{dep} = 30^\circ$, $\varphi_{c,dry} = 45^\circ$.
- The dynamics of the breach evolution predicted by the model, though much slower because of the reduced erodibility of the dam material, is similar to Test #2. Due to the limitation of the SWE assumptions, the model is not able to predict the headcut erosion observed experimentally; in spite of this, the final top width is well reproduced (Figure 4a), even if the enlargement process is faster than in the measurements. In this case, since the dynamics is much slower than in the case of Test #2, this discrepancy does not influence the reservoir emptying very much. In fact, the outflow discharge fits the one registered during the experiments well (Figure 4b), in both shape and peak discharge.
- 361 When values of the erodibility coefficient smaller than 5 $\text{cm}^3/\text{N/s}$ were adopted, the breach 362 formation process was initially too slow, and the increase in the water level upstream caused the 363 overtopping of the whole dam (not limited to the pilot channel) and the consequent widespread erosion, which was never observed in the experiments. This probably happens because the initial evolution of the 364 breach is generated by headcut erosion, which cannot be simulated with SWE models. Hence, only one 365 larger value of k_d was considered in the sensitivity analysis ($k_d = 10 \text{ cm}^3/\text{N/s}$), and numerical results for 366 this simulation are compared with the experiments and with the reference simulation in Figure 4. The 367 breach opening is faster than in the reference simulation, but the final top width is still well caught; the 368 overflow discharge presents a slightly different trend, with a sudden initial increase due to the rapid 369 breach erosion and an underestimated peak value. Also for this test case, a sensitivity analysis on the 370 critical shear stress revealed that this parameter does not influence the model predictions (results not 371 372 shown).
- 373 3.3 Experimental levee breach

The aim of the present test case is to investigate how the erosion model can reproduce the opening of lateral breaches. In particular, one of the field-scale levee breach experimental tests presented by Kakinuma & Shimizu (2014) is considered (Case 4). A 176 m-long and 8 m-wide stretch of the floodway channel of the Tokachi River (Japan), with bottom slope equal to 1/500, was set up by inserting

a vertical wall on the left and by substituting a portion of the existing right levee with a 3 m-high erodible

379 dyke, made of sand with $d_{50} = 0.7$ mm, $d_{30} \approx 0.2$ mm, $d_{90} \approx 40$ mm, $\rho_s = 2650$ kg/m³, p = 0.4. The levee

crest width was equal to 6 m, while the side slopes were both 1V:2H. The inflow discharge was increased

until the levee was overtopped just at the location where a notch (with length 3 m and depth 0.5 m) had

been previously carved to trigger the breach; the outflow discharge inundated a floodable area specifically

arranged (Figure 5a).

The grid size was set at 0.5 m, while Manning's coefficient was assumed equal to 0.023 m^{-1/3}s, as suggested by the experimenters. The measured inflow discharge was set as upstream boundary condition, and a rating curve was imposed downstream far enough to avoid disturbances in the water level at the breach site. The following parameters were assumed for the levee material for the erosion model: $\tau_c = 0.5$ Pa, $k_d = 80 \text{ cm}^3/\text{N/s}$, $\varphi_{c,wet} = \varphi_{dep} = 30^\circ$, $\varphi_{c,dry} = 40^\circ$. The same critical angles were used for the sediment transport model.

390 Experimental observations show that, initially, overflow water starts eroding the downhill slope of the levee, until the top of the front slope is reached, and erosion proceeds downward to the bottom of 391 the levee; then, the breach begins to widen to both sides. However, soon the breach is observed to widen 392 393 at a much higher rate in the downstream direction than in the upstream direction; this is due to the 394 development of a high-velocity flow band near the downstream end of the breach, and of a dead water 395 area near the upstream end, where sedimentation occurs. The asymmetry of the breach final width with 396 reference to the initial notch position is a typical feature of lateral breaches, in contrast with what is 397 usually observed in frontal dam breach test cases. The sediment transport model is able to capture this 398 process, as can be noticed in Figure 5b, where the bed elevation contour maps at selected times are 399 reported to show the breach evolution. On the other hand, the erosion model, which neglects deposition, is not able to reproduce this process in detail; nevertheless, the asymmetry of the breach widening is still 400 predicted, especially in the first stages (see Figure 5c), even if in a less pronounced way than in the 401 402 experimental observations towards the end of the process. Despite these differences in the simulation of the erosion process, the two models predict a similar trend for the total breach width, which is slightly 403 underestimated with reference to the experimental data, as can be noticed in Figure 5d. Breach widening 404 seems to start somewhat late in the sediment transport model simulation, but then evolves at a higher rate 405 406 than in the erosion model simulation. A similar trend can be observed in the outflow discharge time series, reported in Figure 5e. The peak discharge is underestimated by only 4-5% by both models with 407 reference to the measured value. 408

409 A sensitivity analysis on the erodibility parameters was performed. First, the erodibility 410 coefficient was analyzed, and simulations were repeated assuming $k_d = 40$, 60, 80, 100, and 120 cm³/N/s 411 ($\tau_c = 0.5$ Pa). The final breach width is observed to increase with erodibility (simulated values are 8, 33, 412 62, 80, and 127 m, respectively). The smallest erodibility value is probably not representative of the levee 413 material, since overtopping does not generate appreciable erosion; on the other hand, the highest 414 erodibility values overestimate the final breach width, also because erosion is predicted along the inner 415 riverbank (upstream of the breach), and this fact was not observed experimentally. As regards the 416 predicted discharges, Figure 5f compares the outflow hydrographs: the arrival time is slightly anticipated 417 for the highest erodibility values, but the final peak discharge is very similar for $k_d \ge 80$ cm³/N/s.

The sensitivity to the critical shear stress was also analyzed, and τ_c was varied from 0.1 to 0.5 and 1 Pa (maintaining $k_d = 80 \text{ cm}^3/\text{N/s}$). The outflow hydrographs obtained from the three simulations are compared in Figure 5g, showing that the arrival time and the peak discharge are only slightly dependent on the critical shear stress.

422 3.4 Levee breach on the Enza River

The model was finally employed to simulate the recent flood event that took place on the Enza 423 River (Northern Italy), a tributary of the Po River, in order to verify its applicability to real test cases. A 424 425 severe flood event followed the prolonged heavy rainfall occurred on the river basin on December 10-11, 2017, resulting in the highest water levels ever recorded at all the gauging stations along the river. On 426 427 December 12 at 05:30 a.m. water started to overtop the right levee near Lentigione di Brescello (Reggio Emilia), initially triggering three very close breaches, which almost merged into a single large one in 428 time. The overtopped part of the levee was 250 m long, and the total final breach width was 429 430 approximately 160 m, while the widening took about 4 hours. The total flooded area was about 6.3 km², restricted by the levees of the Enza and Po Rivers, by a road embankment and a channel levee (see Figure 431 6a). 432

The terrain elevation was obtained from a digital terrain model (DTM) with resolution equal to 1 433 m, based on a LiDAR survey of the area. The domain was then discretized with square cells of size 2 m \times 434 2 m (approximately 5 million active cells), but the levee crest elevations were preserved after the down 435 sampling of the original DTM. The roughness coefficient was set equal to $0.05 \text{ m}^{-1/3}$ s, after a calibration 436 procedure. The upstream boundary condition is the discharge time series obtained from the conversion of 437 438 measured water levels at the level gauge station of Sorbolo (whose position is reported in Figure 6a). An experimental rating curve was available, but the presence of the breach is expected to influence the level 439 measurements due to the generation of a drawdown profile, thus "invalidating" the rating curve after the 440 breach opening. For this reason, two different stage-discharge relations (before and after the breach) were 441 used to convert the water levels, following the same procedure described by Vacondio et al. (2016). The 442

discharge hydrograph is shown in Figure 6b, together with the water levels in the Po River, imposed
downstream (these were relatively low, and backwater effects were not observed during the event).

The levee is built with silt loam with the following texture: sand 15-39%, silt 49-67%, clay 12-445 18%. The material porosity is equal to 0.4, and the dry specific weight of soil is approximately 1.55 446 Mg/m³. Considering these characteristics, Hanson et al. (2010) suggest an erodibility coefficient in the 447 range 0.5-10 cm³/N/s, while the critical shear stress should be assumed in the range 0.1-1 Pa. Moreover, 448 the formula reported by Wu (2013) for estimating k_d would lead to 2-3 cm³/N/s. The following parameters 449 were then assumed for the levee material for the erosion model: $\tau_c = 1$ Pa, $k_d = 5$ cm³/N/s, p = 0.4, $\varphi_{c,wet}$ 450 $=\varphi_{dep}=30^{\circ}, \varphi_{c,dry}=50^{\circ}$. The erosion equation was applied only in the cells representing the levee (hence 451 the riverbed is never modified), and the bottom elevation of the levee foundation (assumed equal to the 452 453 local terrain elevation outside the river) was also specified, in order to prevent erosion below the ground level. Note that erosion can potentially occur anywhere on the levees; the exact position of the breach 454 does not have to be defined a priori, because the opening occurs where the levee is overtopped. Figure 6c 455 456 reports the longitudinal profile of the (right) levee crest elevation for the 8 km-long stretch of the river downstream of Sorbolo, together with the profiles of the maximum water surface elevations along the 457 river obtained from two different simulations. In the first one the levees are assumed to be non-erodible 458 (bathymetry constant in time in the whole domain), whereas in the second one the bathymetry can change 459 460 accordingly to Equation (7) and to the bank failure algorithm, leading to the breach formation where the 461 levee is overtopped. In the second simulation, the maximum water levels are lowered due either to the 462 drawdown effect induced by the breach upstream or to the reduced discharge downstream. The maximum observed water levels surveyed after the event are also reported at selected locations, and confirm that the 463 flood propagation along the river is correctly reproduced by the model (Figure 6c). Please note that the 464 water levels (both simulated and surveyed ones) are quite close to the levee crest in different locations, 465 but the levee is actually overtopped only where breaches were observed in the field. 466

Figure 7 shows the breach evolution in terms of contour maps of the bottom elevation at selected 467 times (velocity vectors are also reported). Initially, erosion is not concentrated in a restricted area (as in 468 the previous test case), because water overtops the levee crest along roughly 270 m, and the erosion 469 process appears scattered along this length. However, the levee crest elevation is not regular in this area, 470 hence some low points appear more vulnerable to erosion, and give origin to the development of multiple 471 472 small breaches, which enlarge in time. The most vulnerable point is just downstream of the levee bend, and the highest velocities are observed there. The breach takes about 3 hours from the beginning of 473 overtopping to reach its final extension, with only small further modifications in the following 2 hours. 474 475 The total final width is approximately 150 m, separated into five segments along roughly 250 m, the 476 largest of which is 60 m wide. Actually, only three breaches were observed in the field; however, given

477 the uncertainties in boundary conditions, material parameters and terrain elevations, the model correctly

478 predicts the opening of multiple breaches, and captures the overall process quite well. Clearly, any model

- that only employs geometric relations or internal links between river and floodplain to simulate the breachopening would hardly capture this complex behavior.
- The actual total flooded area is reported in Figure 8, compared with the simulation results in terms of maximum water depths reached at 07:00 p.m. (December 12); by this time, operations for draining the flooded volume, which are not included in the simulation, had just started.
- The model sensitivity to erodibility parameters was also analyzed. First, the simulation was 484 485 repeated with a fixed critical shear stress ($\tau_c = 1$ Pa), and the erodibility coefficient was doubled (10 $cm^3/N/s$, halved (2.5 $cm^3/N/s$), and further reduced to 1 $cm^3/N/s$, in order to explore the whole range of 486 variability of this parameter for the given material. The breach evolution for these simulations is 487 compared in Figures 9a-9i. The erodibility coefficient has a significant impact on both the failure time 488 and the breach evolution. When the value of k_d is reduced, the erosion process is slower and less 489 490 pronounced. When k_d assumes the smallest value (1 cm³/N/s), the breach evolution takes 6 hours, and is characterized by a generalized erosion along the whole overtopped length. Results of the simulation with 491 $k_d = 2.5 \text{ cm}^3/\text{N/s}$ are similar to the reference case, even if the opening time slightly increases (4 hours). 492 Surprisingly, while an increase in the value of k_d to 10 cm³/N/s reduces the failure time to only 1.5 hours, 493 494 the total width does not increase compared to the reference simulation. In fact, a single breach is 495 generated: the most vulnerable portion of the levee is eroded very rapidly, and the consequent drop in the 496 water level in the river stops the overtopping and erosion processes along the rest of the levee. A comparison of the breach outflow hydrographs is reported in Figure 9i for these simulations, and shows 497 that, apart from the case with $k_d = 1 \text{ cm}^3/\text{N/s}$ which highly underestimates the outflow discharge (and the 498 total flooded area), for the other values the peak discharge is underestimated by less than 10% compared 499 500 to the reference simulation, and the peak is observed within ± 0.5 hours. The differences in the total 501 outflow volume are always below 10% compared to the reference simulation, except for the case with the 502 lowest value of the erodibility coefficient, for which the volume difference is over 30%.
- A sensitivity analysis to the critical shear stress was also performed, changing its value from 1 Pa to 0.1 Pa, and to 10 Pa, maintaining $k_d = 5 \text{ cm}^3/\text{N/s}$, in order to evaluate its influence on the simulation results. The results confirm, similarly to the previous test cases, that the critical shear stress does not influence the breach evolution significantly, especially in the case of a reduced value assigned to this parameter. The adoption of the highest value, on the other hand, results in a slightly slower erosion process and reduced overflown volume of water (-15%), due to the fact that the predicted bed shear stresses and the critical value are of the same order of magnitude (10¹ Pa). Finally, the sensitivity to the

critical angles for slope stability was also analyzed, but their influence on the simulation results is notevident for this test case (results not shown).

512 The flood event was also simulated using the sediment transport model described in Appendix A. The following parameters were assumed for the levee material: $d_{50} = 0.04$ mm, $d_{90}/d_{30} = 10$, $\rho_s = 2650$ 513 kg/m³. Sediment transport was allowed only in a wide region around the breach, not only to reduce the 514 computational burden, but also to better compare the two models. A single breach develops rapidly after 515 levee overtopping: the failure time is less than 1 hour, and the final width is 65-75 m (a map of the breach 516 site is reported in Figure 10). Actually, a similar behaviour can be obtained from the erosion model if the 517 518 erodibility coefficient is increased to $50 \text{ cm}^3/\text{N/s}$, which however is no longer representative of the levee material. In fact, it must be stressed that a bedload transport model is not expected to describe the 519 complex behavior of the erosion process in a levee built with cohesive material. 520 With regard to the simulation time, the erosion model takes 1.3 h to simulate 2 days of physical 521 time on a P100 Tesla® GPU, resulting in a ratio of physical to computational time equal to 37. Compared 522 523 to an analogous simulation where the levee breach on the Enza River is modelled using a geometric approach (similarly to Vacondio et al., 2016), the computational overhead is negligible (3%). The 524

sediment transport model takes 2.8 h on the same device (physical/computational time = 17). The good

526 performance of GPU-accelerated models for high-resolution simulations is thus confirmed, and this

527 makes the application of these models to complex real field test cases particularly convenient.

528 4 Discussion

529 The main aim of the present work is to introduce a tool able to automatically handle the possible opening of one or more levee breaches due to overtopping in a state-of-the-art 2D numerical code for 530 flood propagation. The need to define the breach dimensions and position as input parameters is avoided 531 by introducing an equation that predicts the bottom erosion wherever the local value of the bed shear 532 stress exceeds a critical value (in the practice, this coincides with the occurrence of levee overtopping). 533 534 The model was validated by simulating experimental test cases and one real flood event, and the 535 numerical results were in good agreement with the measurements. In particular, the application to the 536 historical test case of December 2017 on the Enza River, presented in Section 3.4, shows that the 537 proposed model can effectively simulate this kind of problems: the breach position is correctly identified, and the opening of multiple breaches can be captured; moreover, the predicted outflow hydrograph from 538 the breach results in a well-reproduced flooded area. 539

540 Clearly, the proposed model does not capture the breach process in detail, because some of the 541 many interrelated factors influencing the breach dynamics are neglected. The simplifications introduced 542 in the model must be kept in mind (most of them are common to other simplified approaches). Among

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543 these, it is worth recalling that a hydrostatic pressure distribution is assumed in the depth-averaged model, 544 while vertical accelerations and streamline curvatures are often non-negligible at the breach site, 545 especially in the case of headcut erosion in cohesive embankments. Moreover, other factors that may increase the bed shear stress or reduce the levee resistance to erosion, such as sediment concentration, 546 infiltration processes, etc., are not considered in the present model. Despite these simplifications, the final 547 breach width and peak outflow discharge are predicted reasonably even in the case of cohesive 548 embankments, as shown by results from Test #10 in Section 3.2. Finally, the model assumes that the 549 eroded material is washed away by the flow (i.e. sediment deposition is not simulated). This may slightly 550 551 influence the breach configuration, especially in the case of non-cohesive materials (see for example Figure 5), and the effect is more evident for small-scale experimental test cases. However, for real field 552 simulations, this hypothesis does not probably have much impact on the overall process. 553

The influence of the levee material on the erosion process is taken into account by means of two 554 model parameters, the erodibility coefficient and the critical shear stress. Although their definition is not 555 556 straightforward, some indications from the literature allow identifying the plausible range of variability of their values. The sensitivity analyses performed for several test cases show that the critical shear stress 557 does not influence the model results significantly, because the bed shear stresses largely exceed the 558 559 critical value during overtopping. On the other hand, the erodibility coefficient must be defined more 560 carefully, especially in the case of non-cohesive material, for which its range of variability can be quite 561 large. The analyses conducted in this study show that the breach width is affected by the value assigned to 562 this parameter, while the outflow hydrograph is somewhat less influenced (as long as the value of k_d is representative of the material type), as can be noticed from results reported in Section 3.3. Similar 563 564 considerations are true for the case of a cohesive material (see results from Section 3.4). This is encouraging, since the outflow hydrograph is the most relevant outcome of the model when the aim of the 565 simulation is the prediction of the levee breach-induced flooding. 566

In all tests simulated in the present work, the embankment is considered homogeneous, meaning 567 that a unique value of the erosion model parameters is adopted for the whole domain, but different values 568 can easily be assigned to different segments of the levee; scour-dependent parameters could also be used 569 in order to model stratified embankments. In general, however, real levees are heterogeneous, and data 570 concerning the spatial distribution of the material type are often lacking, hence assigning a unique 571 "average" value to the model parameters can be considered reasonable in the practice. A possible 572 enhancement to this approach can be the inclusion of the presence of a grass cover, which protects the 573 levee surface and delays the beginning of the erosion process, reducing the probability of levee failure 574 575 (Mazzoleni et al., 2017). This effect can be achieved by increasing the critical shear stress, or by adjusting 576 Manning's coefficient (as done by Viero et al., 2013), during the first stages of overtopping. Finally, a

scour-dependent erodibility coefficient could be used to distinguish between the embankment material
and the levee foundation material, when this cannot be assumed as non-erodible. These modifications to
the proposed model will be considered in future works.

580 Results obtained with the erosion model were also compared with the predictions of a simple sediment transport model that integrates the Exner equation for bedload transport. The main drawbacks of 581 this latter model were found to be not only the greater complexity and computational effort required, but 582 583 more importantly its inadequacy for simulating the erosion of cohesive levees. Moreover, even in the case 584 of a non-cohesive material, a sediment transport model may overestimate the embankment erosion 585 process. In fact, experimental observations show that a fine sand is more resistant to erosion than a coarse sand, due to its "apparent cohesion" (Evangelista, 2015; Pickert et al., 2011), while bedload transport laws 586 usually assume that the transport capacity increases when the size of particles decreases. More 587 sophisticated sediment transport models could be employed, but only at the cost of introducing a larger 588 number of model parameters and of further increasing the computational time. For these reasons, the 589 590 employment of this kind of models does not seem justified for simulating the flooding triggered by levee breaches in very large domains. 591

Finally, the efficiency of the proposed model must be stressed. Previous works (e.g. Vacondio et al., 2014) already assessed that a speed-up up to two orders of magnitude can be obtained using GPUaccelerated models (as PARFLOOD) instead of serial codes. The implementation of the proposed erosion model does not degrade the computational efficiency compared to the adoption of a simple geometric approach, and requires a lower computational time than a sediment transport model.

597 **5 Conclusions**

In this paper, a 2D SWE code was coupled with an erosion model that allows simulating the opening of levee breaches generated by overtopping, without the need to set the breach position and dimensions as input parameters. The breach evolution was predicted correctly for all tests used for model validation, which concerned both cohesive and non-cohesive materials. Therefore, the model can be particularly useful to create flood hazard maps and to support the design and verification of existing levee systems, also thanks to the high computational efficiency of the GPU implementation.

604

605 Appendix A. Sediment transport model

A simple bedload transport model was also developed for comparison purposes. The sediment transport model was taken from the literature, and the implementation of Juez et al. (2014) was adopted, also because it can be efficiently coded for GPUs. The model is based on the integration of the Exner equation, hence only bedload transport is considered; moreover, an approach where SWE and the

- 610 morphodynamic equation are uncoupled is chosen (in order to reduce model complexity). For the
- hydrodynamic part, the model described in Section 2.1 is adopted. Here, only the main features of the
- 612 sediment transport model are briefly recalled.
- 613 The bed evolution is described by the 2D Exner equation:

$$614 \qquad \frac{\partial z}{\partial t} + \frac{1}{1-p} \frac{\partial q_{s,x}}{\partial x} + \frac{1}{1-p} \frac{\partial q_{s,y}}{\partial y} = 0,\tag{A1}$$

- 615 where $q_{s,x}$ and $q_{s,y}$ are the bed load discharges in the x and y directions, respectively, which can be
- expressed by any sediment transport formula; in this work, Smart equation (Smart, 1984) is adopted:

617
$$\Phi = 4(d_{90}/d_{30})^{0.2} FS^{0.1} \theta^{0.5} (\theta - \theta_c^{SM}).$$
(A2)

618 In Eq. (A2), Φ is the dimensionless sediment discharge, computed according to the following expression:

619
$$\Phi = \frac{|q_s|}{\sqrt{g(s-1)d_m^3}},$$
 (A3)

- 620 where $s = \rho_s / \rho$ is the ratio of the material density ρ_s to the water density ρ , and d_m is the mean sediment
- diameter. Moreover, Eq. (A2) contains the Shields parameter θ (i.e. the dimensionless shear stress τ),
- 622 defined as follows:

623
$$\theta = \frac{\tau}{g(\rho_s - \rho)d_m},\tag{A4}$$

- 624 and θ_c^{SM} is its critical value according to Smart (1984); d_{90} and d_{30} are the grain sizes at which 90% and
- 625 30% by weight of material is finer, *F* is the Froude number, and *S* is the friction slope. Equation (A2) is 626 applied only when $\theta > \theta_c^{SM}$ (otherwise $\Phi = 0$).
- 627 The bed elevation is updated as follows:

628
$$z_{i,j}^{n+1} = z_{i,j}^n - \frac{\Delta t}{\Delta x} \left(q_{s,i+\frac{1}{2},j}^* - q_{s,i-\frac{1}{2},j}^* \right) - \frac{\Delta t}{\Delta y} \left(q_{s,i,j+\frac{1}{2}}^* - q_{s,i,j-\frac{1}{2}}^* \right), \tag{A5}$$

where q^*_s represents the "sediment" flux at each intercell. Only the computation at the intercell between cells (i,j) and (i+1,j) is reported in the following (for the other three fluxes, similar expressions can be used). Flux is calculated as:

632
$$q_{s,i+\frac{1}{2},j}^{*} = \begin{cases} \frac{1}{1-p} q_{s,x,i,j} & \text{if } \tilde{\lambda}_{s} > 0\\ \frac{1}{1-p} q_{s,x,i+1,j} & \text{if } \tilde{\lambda}_{s} \le 0 \end{cases}.$$
 (A6)

633 The "sediment" celerity $\tilde{\lambda}_s$ is estimated as:

634
$$ilde{\lambda}_s = \frac{\delta q_{s,x_s}}{\delta z},$$
 (A7)

- 635 where $\delta q_{s,x} = q_{s,x,i+1,j} q_{s,x,i,j}$, and $\delta z = z_{i+1,j} z_{i,j}$.
- The bank failure algorithm presented in Section 2.3 is also added to the model.

637

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- 646

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Table 1. Main features for the 2D frontal breach test cases by HR Wallingford (Tests #2 and #10).

Test	#2	#10
Material type	Sand	Clay
$d_{50} ({ m mm})$	0.25	0.005
Dam height (m)	0.50	0.60
Crest width (m)	0.20	0.20
Side slopes	1V:1.7H	1V:2H
Initial reservoir level (m)	0	0.58
Pilot channel depth (m)	0.02	0.05
Pilot channel width (m)	0.15	0.50

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808	Table 2. Sensitivity analys	s on the model parameters for	Test #2 by HR Wallingford. The
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reference simulation was performed adopting $n_f = 0.018 \text{ m}^{-1/3}\text{s}$, $\tau_c = 10^{-2} \text{ Pa}$, $k_d = 150 \text{ cm}^3/\text{N/s}$, $\alpha_{creat} = \alpha_{creat} = 30^\circ$, $\alpha_{creat} = 45^\circ$

810	$\varphi_{c,wet} =$	φ_{dep}	$= 30^{\circ}$, $\varphi_{c,dry}$	= 45°.

Case	Peak discharge (m ³ /s)	% Error (meas.)	% Error (ref.)	Final top width (m)	% Error (meas.)	% Error (ref.)
Measured	0.91	-	-	3.75	-	-
Reference simulation	0.63	-31%	-	3.73	-1%	-
$k_d = 100 \text{ cm}^3/\text{N/s}$	0.54	-41%	-14%	3.23	-14%	-13%
$k_d = 200 \text{ cm}^3/\text{N/s}$	0.68	-25%	8%	4.01	7%	8%
$\tau_c = 10^{-1} \text{ Pa}$	0.63	-31%	0%	3.73	-1%	0%
$\tau_c = 10^{-3} \text{ Pa}$	0.63	-31%	0%	3.73	-1%	0%
$\varphi_{c,wet} = \varphi_{dep} = 25^{\circ}$	0.64	-30%	1%	3.65	-3%	-2%
$\varphi_{c,wet} = \varphi_{dep} = 35^{\circ}$	0.62	-32%	-2%	3.7	-1%	-1%
$\varphi_{c,dry} = 40^{\circ}$	0.68	-25%	8%	4.15	11%	11%
$\varphi_{c,dry} = 50^{\circ}$	0.57	-37%	-10%	3.23	-14%	-13%
$\varphi_{c,dry} = 60^{\circ}$	0.49	-46%	-22%	2.39	-36%	-36%
$\varphi_{c,dry} = 70^{\circ}$	0.35	-62%	-44%	1.54	-59%	-59%
$n_f = 0.016 \text{ m}^{-1/3} \text{s}$	0.60	-34%	-5%	3.64	-3%	-2%
$n_f = 0.020 \text{ m}^{-1/3} \text{s}$	0.64	-30%	2%	3.81	2%	2%

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Figure 1. 1D frontal dam breach test. Experimental dam profiles and numerical results with the sediment transport model, assuming different values for Manning's coefficient n_f (in m^{-1/3}s), at t

- 815 = 30 s (a), and t = 60 s (b). The dashed line represents the initial dam profile.
- Figure 2. 1D frontal dam breach test. Sensitivity analysis on the erodibility coefficient k_d (in
- 817 cm³/N/s) with the erosion model: dam profiles at t = 30 s (a), and at t = 60 s (b), and overflow
- discharge (c). The discharge predicted by the Exner based model is also reported in (c) for
- 819 comparison. The dashed line represents the initial dam profile.

Figure 3. Test #2 by HR Wallingford: (a) Sketch of the experimental set-up (dimensions for Test #10 in brackets). (b)-(e) Simulated breach evolution in time, represented by the bottom elevation maps at selected times, and velocity vectors map. (f)-(g) Experimental and numerical breach top width evolution in time (f), and discharge exiting through the breach (g); the inflow discharge is also represented in (g); numerical results are reported for three different values of the erodibility coefficient k_d (in cm³/N/s).

- **Figure 4**. Test #10 by HR Wallingford. Experimental and numerical (a) breach top width
- evolution in time, and (b) discharge exiting through the breach. The inflow discharge is also

represented. Numerical results are reported for two different values of the erodibility coefficient

- 829 k_d (in cm³/N/s).
- Figure 5. Levee breach experiment. (a) Sketch of the test set-up. (b-c) Breach evolution in time,

represented by bottom elevation maps at selected times, as predicted by the sediment transport

model (b), and by the erosion model (c). (d) Breach width evolution in time (experimental and

numerical). (e) Discharge exiting through the breach (experimental and numerical). (f-g)

Bischarge exiting through the breach: results of the sensitivity analysis on the erodibility

coefficient k_d (in cm³/N/s) (f), and on the critical shear stress τ_c (in Pa) (g). The inflow and

outflow discharge time series in the channel are also reported in panels (e-f-g).

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Figure 6. Levee breach on the Enza River. (a) Sketch of the study area: the Enza and Po Rivers

- (blue), the levees (yellow), the breach location (red), the main residential and industrial areas
- (black), and the flooded area (cyan) are identified on an orthoimage. (b) Discharge time series
- 841 imposed as upstream boundary condition, and water levels imposed downstream. (c)
- Longitudinal profile of the (right) levee crest elevation and of the maximum water surface elevations obtained from simulations with and without the breach erosion. The maximum
- elevations obtained from simulations with and without the breach erosion. The max
- surveyed water levels at selected locations are also reported for comparison.
- **Figure 7**. Levee breach on the Enza River. Contour maps of the simulated bottom elevation and

vector maps of the velocity in the breach zone at selected times: (a) 0.5 h, (b) 1 h, (c) 1.5 h, and

- (d) 5 h after the beginning of overtopping. Only one vector out of 9 is represented for the sake of
- clarity. The red contour line identifies the wet/dry front.
- **Figure 8**. Levee breach on the Enza River. Contour map of the simulated maximum water depth (up to 07:00 p.m., December 12), and actual total flooded area (white line).
- **Figure 9**. Levee breach on the Enza River: sensitivity analysis on the erodibility coefficient. (a)-
- (i) Contour maps of the bottom elevation in the breach zone at selected times for the different

- simulations: (a)-(c) $k_d = 10 \text{ cm}^3/\text{N/s}$; (d)-(f) $k_d = 2.5 \text{ cm}^3/\text{N/s}$; (g)-(i) $k_d = 1 \text{ cm}^3/\text{N/s}$. (j) Simulated
- outflow hydrographs from the breach for different values of the erodibility coefficient k_d (expressed in cm³/N/s).
- **Figure 10**. Levee breach on the Enza River. Contour map of the final bottom elevation in the
- breach zone obtained from the sediment transport model.