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ARTICLE

Aggregates of quadrupolar dyes for two-photon absorption: the role of intermolecular interactions

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We present a theoretical investigation of small aggregates of quadrupolar (A- π -D- π -A or D- π -A- π -D) charge-transfer dyes, focusing the attention on the role of intermolecular interactions on optical properties. We tackle the theoretical issue adopting essential-state models (ESMs), that describe the isolated molecule in terms of a minimal number of electronic states, corresponding to the resonance structures. ESMs quite naturally describe intermolecular interactions relaxing the dipolar approximation and accounting for molecular polarizabilities. The approach is applied to curcuminoid and squaraine dyes, two families of chromophores with weak and strong quadrupolar character, respectively. The method is validated against experiment and for curcuminoids also against time-dependent density functional theory. ESMs rationalize the strong ultra-excitonic effects recurrently observed in experimental optical spectra of aggregates of highly polarizable quadrupolar dyes, offering a valuable tool to exploit the supramolecular design of material properties.

Introduction

Intermolecular electrostatic interactions are the driving force of two key phenomena in molecular functional materials: energy transfer and energy delocalization. Energy transfer is an incoherent process where an excited molecule, the energy donor, transfers its excess energy to a nearby energy acceptor.^{1–3} Being driven by long-range electrostatic interactions, energy transfer occurs up to comparatively large distances (~ 100 Å) and requires the resonance between the de-excitation energy of the donor (from its relaxed excited state) and the absorption energy of the acceptor. Energy delocalization instead occurs when electrostatic interactions are larger than the difference between the transition energies of nearby molecules, giving rise to Frenkel excitons.^{4,5} Energy delocalization governs the spectral properties of molecular crystals and aggregates, where intermolecular distances can be comparable to or even smaller than the sum of Van der Waals radii. The simplest models for either phenomenon rely on the dipolar approximation for intermolecular interactions, directly relating the two processes and their measurable effects to experimentally accessible data for the isolated molecules, and specifically to the transition dipole moments of the relevant excitations. As originally derived by Förster,^{6,7} the rate of energy transfer (often called Förster resonance energy transfer, FRET) goes with the product of the squared transition dipole moments for the emission of the

energy donor and the absorption of the energy acceptor, while the exciton splitting in a dimeric structure (or the exciton band-width in a molecular crystal) is proportional to the inner product of the transition dipole moments of nearby molecules.^{4,5} Therefore, in the dipolar approximation, only optically allowed states (i.e. states having a sizable transition dipole moment from the ground state) are of relevance either for energy-transfer processes or for exciton delocalization. However, the dipolar approximation fails whenever intermolecular distances are comparable to or smaller than the molecular dimensions: the involvement of *dark* (optically forbidden) states in energy transfer processes has been extensively discussed in the literature,^{8–12} and several suggestions have been given about exciton coupling of dark states.^{13,14} A second, somewhat subtler approximation usually enters the standard models for either energy transfer or energy delocalization, and amounts to neglecting the molecular polarizability. In other terms, it is assumed that the charge distribution on each molecule, in the ground or in the excited state, is not affected by the presence of nearby molecules, a fairly poor approximation for largely polarizable molecules in molecular aggregates and crystals where intermolecular distances are small.^{15,16}

In this context, charge-transfer (CT) dyes, a large family of π -conjugated molecules where the presence of electron donor (D) and/or acceptor (A) groups leads to low-energy excitations with large polarizabilities, are particularly interesting. The low-energy physics and the linear and nonlinear optical properties of CT dyes are well captured by essential-state models (ESM)^{17–24}, a family of parametric Hamiltonians that describe the electronic structure of CT dyes in terms of a few diabatic basis states, corresponding to the main resonating structures. The coupling to molecular vibrations and polar solvation leads to a quite accurate description of the

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complex spectral behavior of these molecules in different environments. ESMs also quite naturally describe intermolecular interactions relaxing the dipolar approximation, fully accounting for the molecular polarizability.^{14–16,25} The applicability of ESMs to energy-transfer processes has been validated by a direct comparison with time dependent density functional theory (TDDFT) calculations.^{12,26} The reliability of ESMs to describe the effects of intermolecular interactions in linear and nonlinear optical spectra of a few model systems has been validated experimentally.^{14,27–34} For aggregates or crystals of polar (D- π -A) dyes, ESMs predict strong ultra-excitonic effects,¹⁶ eventually leading to multiexciton generation¹⁵ and phase coexistence,^{35–37} while biexciton states in aggregates of quadrupolar (D- π -A- π -D or A- π -D- π -A) dyes have been suggested as a way towards amplified two-photon absorption (2PA).¹⁴

In this paper, we apply ESMs to aggregates of quadrupolar dyes, validating the results against quantum chemical calculations. The models are subsequently exploited as a reliable and flexible tool to understand the spectral properties of organic nanoparticles based on quadrupolar dyes. Indeed, quadrupolar dyes are actively investigated as structures of choice for 2PA applications in bioimaging, nanofabrication, photodynamic therapy, etc. Typical 2PA dyes include squaraines,^{38–45} fluorene-based chromophores,^{46–51} distyrylbenzenes,^{52–54} to name a few. These dyes, designed for large 2PA cross sections, are in general poorly soluble in water and biological media. Different strategies (including e.g. encapsulation in micelles,⁵⁵ dispersion in silica nanoparticles,⁵⁶ preparation of supramolecular assemblies⁵⁷) are exploited to make hydrophobic dyes suitable for biological applications. Among different methods, organic nanoparticles (ONPs) offer a simple and versatile approach to disperse nano-sized agglomerates of dyes in water.^{57–61} For applicative purposes, it is important that ONPs are stable and maintain or possibly improve the optical properties of the dye. Specifically, for 2-photon imaging applications, the active species must have a large 2PA cross section and a large fluorescence quantum yield, a delicate issue for ONPs in view of the self-quenching of fluorescence often observed in condensed phases. Nevertheless, several interesting examples of fluorescent organic nanoparticles (FONs) are known with large fluorescence quantum yields,^{58,60,62} and sometimes amplified 2PA response.⁵⁹ However, most ONPs based on quadrupolar dyes show a strongly reduced fluorescence.^{63–65} In this work will set the basis to understand this phenomenon, offering suggestions for the optimized design of aggregates of quadrupolar dyes. We will focus the attention on two different families of chromophores: boron-difluoride-curcuminoids

(hereafter curcumins, see **1** in Fig. 1) and squaraines (see **2** and **3** in Fig. 1). Curcumins offer the possibility to validate the essential-state approach not only against the experiment, but also against TDDFT calculations. Squaraines were selected as interesting systems showing unusual aggregation effects^{40,41,66} even if the well-known problems of TDDFT in dealing with squaraines^{67–69}, hinders a thorough computational analysis of these systems.

Theoretical methods

TDDFT Calculations

Ground-state geometry optimizations were performed using density functional theory (DFT), as implemented in GAUSSIAN09⁷⁰ software package using the 6-31+g(d) basis set for all atoms. We confirmed the stability of the obtained geometries by ruling out the presence of unstable vibrational mode. The ground-state geometry of the isolated molecule **1** in gas phase was optimized employing B3LYP (Becke, three parameter, Lee–Yang–Parr)⁷¹ hybrid exchange and correlation energy functional, while the long-range dispersion corrected non-local energy functional, ω B97XD,⁷² was employed for the geometry optimizations of dimers to account for dispersion corrections. Solvation effects in dichloromethane (DCM) were included adopting the polarizable continuum model (PCM).⁷³

TDDFT calculations were performed using the long-range corrected (LRC) version of B3LYP, the Coulomb-attenuating method (CAM-B3LYP)⁷⁴ and 6-31+g(d) basis set. We used the LRC density functional to properly describe CT states. TDDFT calculations were run for **1** in gas phase and DCM solvent. Moreover, we studied two different molecular dimers, whose geometries were extracted from the crystal structure. The evolution with the intermolecular distance of the spectral properties of both dimers was investigated.

The transition intensity for the linear (one photon) absorption (1PA) is expressed in terms of the oscillator strength (atomic units):

$$f = \frac{2\omega_n}{3} |\langle 0 | \mu | n \rangle|^2$$

where ω_n is the excitation frequency of the $|n\rangle$ state and μ is the electric dipole moment operator.

The DALTON2015 package⁷⁵ was used to calculate two-photon absorption (2PA) spectra of **1** in gas phase and in solution and of molecular dimers in gas phase, using CAM-B3LYP functional and the 6-31+g(d) basis set. The 2PA intensity (δ_{2PA}) is calculated, for a linearly polarized monochromatic beam of light, as follows:^{76–78}

$$\delta_{2PA}(\omega) = \sum_{kl} 2S_{kk}(\omega) S_{ll}(\omega) + 4S_{kl}(\omega) S_{kl}(\omega)$$

where $S(\omega)$ is the 2PA tensor.⁷⁵ The 2PA cross section is finally obtained (assuming a Lorentzian bandshape) as:

$$\sigma_{2PA}(\omega) = \frac{4\pi^3 \alpha a_0^5 \omega^2}{15c \Gamma} \delta_{2PA}(\omega)$$

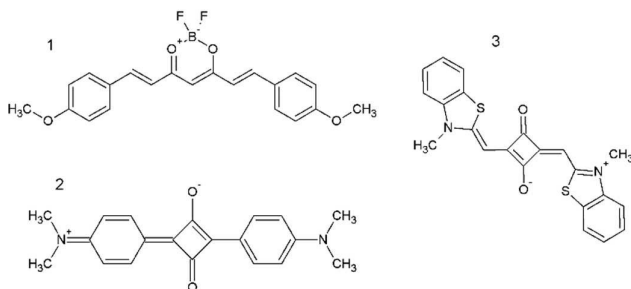


Fig. 1. Structures of the investigated molecules.

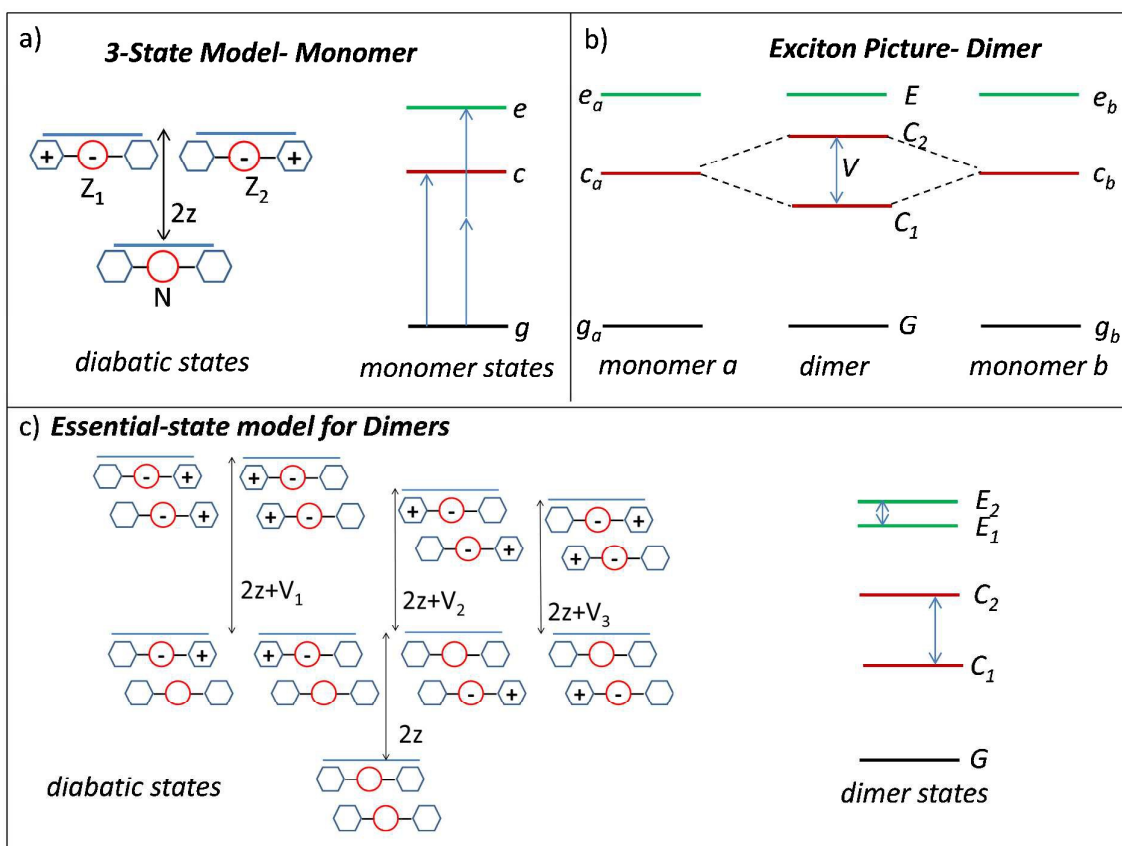


Fig. 2. Panel a: Sketch of the 3-state model for quadrupolar dyes. Panel b: the exciton picture for a dimer. Panel c: ESM for a dimer. Complete expressions for electrostatic interactions are reported in the Supporting Information (Fig. S1 and S2).

where a_0 , c and α are the Bohr radius, the speed of light and the fine structure constant, respectively, while Γ (set to 0.1 eV) is the full width at half maximum of the Lorentzian lineshape.

ESM for quadrupolar dyes and their aggregates

The 3-state model for quadrupolar dyes¹⁹, proposed in 2006, has been validated against experimental data for several families of quadrupolar dyes, including fluorene-based dyes, squaraines, substituted distyrylbenzenes, cyanines, etc.^{27,79–82}. More recently, the 3-state model has been extended to account for a fourth state, as relevant for cyanine dyes.⁸³ The 3-state model for an isolated D- π -A- π -D (or equivalently A- π -D- π -A) quadrupolar dye considers three diabatic basis states, corresponding to three main resonating structures: the neutral state N , and two degenerate zwitterionic states, Z_1 and Z_2 , as sketched in panel a of Fig. 2. Only two parameters enter the electronic model: 2η , the energy gap between the two degenerate zwitterionic states and the neutral state, and τ , the mixing element between N and both Z_1 and Z_2 . The dipole moment operator has only two non-vanishing terms, corresponding to the permanent dipole moments of Z_1 and Z_2 , which are aligned along the molecular axis and have opposite directions for the two states. The model parameter μ_0 represents the magnitude of the permanent dipole moment of Z_1 and Z_2 , and it is required to calculate the intensity of optical spectra.

A symmetrized basis set is conveniently introduced: N and $Z_{\pm} = (Z_1 \pm Z_2)/\sqrt{2}$. On this basis, the ground state, g , is a

linear combination of N and Z_{\pm} , with the weight of Z_{\pm} and measures the quadrupolar character of the dye, i.e. the charge residing on the central group: $\rho = 0.5(1 - \eta/\sqrt{\eta^2 + 2\tau^2})$. Two excited states are obtained with opposite parity: a bright *ungerade* state c , corresponding to Z (which remains unmixed), and the dark *gerade* state e , the N and Z_{\pm} combination orthogonal to g .

This simple three-state electronic model captures the essential features of quadrupolar dyes, with the bright state located at lower energy than the dark, 2PA-active state. More in detail, dyes with low ρ values ($2\eta/\tau \gg 1$) have almost degenerate 1PA-active (c) and 2PA-active (e) states, driving the system towards excited-state symmetry breaking (class I dyes).¹⁹ Dyes with high ρ values ($2\eta/\tau \ll 1$) have a small energy gap between the ground and the 1PA-active state, leading the system towards a ground-state instability (class III dyes).⁷⁹ Systems with intermediate ρ ($2\eta \approx \tau$) have the 1PA-active state lying almost midway between the ground state and the 2PA-active state, with amplified 2PA and no tendency to symmetry breaking (class II).¹⁹

The exciton model is the prevailing approach to intermolecular interactions in molecular aggregates or crystals and, as sketched in Fig. 2b, it corresponds to a zeroth-order perturbative treatment of intermolecular interactions. Accordingly, only degenerate states are mixed by the interaction, leading to the splitting of the two singly-excited states in a dimer and to the formation of the single-exciton band in molecular crystals or large aggregates. The exciton model fully neglects the molecular polarizability, and does not account for

Table 1. Experimental data from Ref. ⁶³ and TDDFT results for curcumin 1.

	Experimental data in Ref. ⁶³			Calculated (gas phase)			
	Transition wavelength (energy)	Molar extinction coefficient ($M^{-1}cm^{-1}$)	σ_{2PA} (GM) ^a	Transition wavelength (energy)	Oscillator Strength	Nature of transitions	σ_{2PA} (GM) ^a
$g \rightarrow c$	488 nm (2.54 eV)	75480	< 10	378 nm (3.28 eV)	2.11	$h \rightarrow l$ (90%)	17
$g \rightarrow e$	385 nm (3.22 eV)	~10000	155	304 nm (4.08 eV)	0.08	$h-1 \rightarrow l$ (90%)	2030

^a GM = Göppner-Mayer. 1 GM = $10^{-50} cm^4 s photon^{-1}$

any charge redistribution in the molecule as a result of the interactions. This is a particularly poor approximation for largely polarizable molecules. The dipolar approximation for intermolecular interactions is a further common approximation adopted in the exciton model. As sketched in Fig. 2b for dimers of quadrupolar dyes, in the dipolar approximation the 2PA-active states are not affected by aggregation phenomena.

ESMs easily overcome both approximations. Specifically, as sketched in Fig. 2c for a molecular dimer, diabatic basis states are constructed for the aggregate as the direct product of the monomers' states. On this basis, the Hamiltonian for the aggregate is easily obtained from the molecular Hamiltonian, with electrostatic intermolecular interactions affecting the energy of basis states where two or more molecules are in a zwitterionic state. The diagonalization of the diabatic Hamiltonian yields to adiabatic states fully accounting for electrostatic intermolecular interactions as well as for the molecular polarizability (see Fig. 2c).

Different approaches can be adopted to estimate electrostatic interactions among diabatic states. Here the electrostatic interactions are described in terms of interaction among integer point-charges at the D and A sites of the zwitterionic basis states (see Fig. S1 and S2 of SI for explicit expressions). The resulting extended-dipole approximation represents a simple but effective way to describe interactions between molecules whose dimensions are comparable to the intermolecular distance.^{9,11,12,15,25,26}

We stress here that electrostatic intermolecular interactions entering the ESMs are relevant to the diabatic state, i.e. the basis states. These states, corresponding to the main molecular resonating structures, are characterized by integer charges. However, the states relevant to spectroscopy are the adiabatic eigenstates, typically characterized by fractional charges. For example, the ground state charge distribution for each dye is defined as $D^{+\rho/2}A^{-\rho/2}$ with ρ values comprised between 0 and 1 ($\rho \sim 0.2$ for curcumin dyes and $\rho \sim 0.3-0.5$ for squaraine dyes).

The number of diabatic basis states for aggregates of quadrupolar dyes increases as 3^N , where N is the number of molecules, so that fairly large aggregates can be easily described, particularly in view of the sparse nature of the Hamiltonian matrix. In the following, we will describe optical spectra calculated for aggregates of different size, imposing open boundary conditions and only accounting for nearest-neighbor interactions. One-photon absorption and fluorescence spectra are calculated assigning Gaussian lineshapes to allowed transitions with full-width at half

maximum Γ . Two-photon absorption spectra are calculated using the SOS expression,^{84,85} where the sum runs over all electronic excited states.

Validating ESM via TD-DFT calculations: the case of curcumine dyes

Modeling the isolated molecules

A recent paper⁶³ reports on spectral properties of nanoparticles of boron-difluoride-curcuminoids (hereafter curcumins). Curcumins

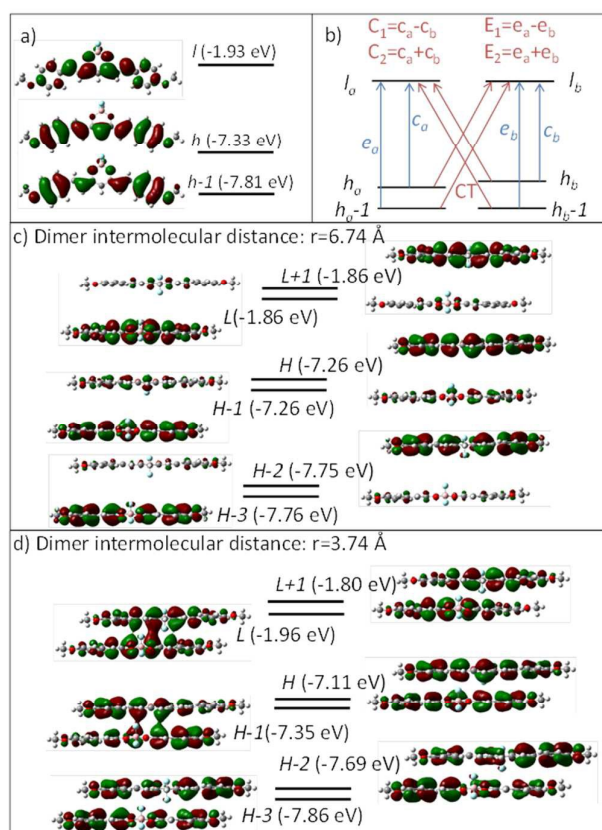


Fig. 3. (a) Frontier molecular orbitals of monomer of 1; (b) sketch of the transitions expected for the dimer based on the monomer frontier orbitals; (c) Frontier molecular orbitals of the dimer at $r = 6.74 \text{ \AA}$; (d) Frontier molecular orbitals of the dimer in the crystallographic geometry ($r = 3.74 \text{ \AA}$).

Table 2. TDDFT results for the P-P dimer at $r = 6.74 \text{ \AA}$

Transition	Energy [eV]	Oscillator strength	δ_{2PA} [a.u.] (σ_{2PA} [GM])	Nature of the transition (>15%)
$S0 \rightarrow S1$ (C_1)	3.20	0.00	3883 (29)	H-1 \rightarrow L (29%) c_a H \rightarrow L+1 (28%) c_b H-1 \rightarrow L+1 (16%) CT H \rightarrow L (17%) CT
$S0 \rightarrow S2$ (C_2)	3.34	4.05	0.41 (-)	H-1 \rightarrow L (44%) c_a H \rightarrow L+1 (45%) c_b
$S0 \rightarrow S3$ (E_1)	4.04	0.15	48.80 (-)	H-3 \rightarrow L (33%) e_a H-2 \rightarrow L+1 (31%) e_b
$S0 \rightarrow S4$ (E_2)	4.11	0.00	2.5×10^5 (3090)	H-3 \rightarrow L (44%) e_a H-2 \rightarrow L+1 (46%) e_b
$S0 \rightarrow S5$	4.27	0.00	0.25 (-)	H \rightarrow L (77%) CT
$S0 \rightarrow S6$	4.28	0.00	0.24(-)	H-1 \rightarrow L+1 (78%) CT

Table 3. TDDFT results for the P-P dimer at $r = 3.74 \text{ \AA}$

Transition	Energy [eV]	Oscillator strength	δ_{2PA} [a.u.] (σ_{2PA} [GM])	Nature of the transition (>15%)
$S0 \rightarrow S1$ (C_1)	3.00	0.00	4907 (32)	H \rightarrow L (72%) c_a - c_b , CT H-1 \rightarrow L+1 (17%) c_a - c_b , CT
$S0 \rightarrow S2$ (C_2)	3.35	3.62	0.53 (-)	H \rightarrow L+1 (66%) c_a + c_b , CT H-1 \rightarrow L (18%) c_a + c_b , CT
$S0 \rightarrow S3$	3.60	0.34	4.69 (-)	H-1 \rightarrow L (74%) c_a + c_b , CT H \rightarrow L+1 (18%) c_a + c_b , CT
$S0 \rightarrow S4$	3.66	0.00	1459.4 (14)	H-1 \rightarrow L+1 (73%) c_a - c_b , CT H \rightarrow L (19%) c_a - c_b , CT
$S0 \rightarrow S5$ (E_1)	3.94	0.10	4.40(-)	H-2 \rightarrow L (57%) e_a - e_b , CT H-3 \rightarrow L+1 (22%) e_a - e_b , CT
$S0 \rightarrow S6$ (E_2)	4.11	0.00	2.04×10^5 (2520)	H-2 \rightarrow L+1 (52%) e_a + e_b , CT H-3 \rightarrow L (36%) e_a + e_b , CT

show a marginal absorption solvatochromism and a well-pronounced emission solvatochromism.^{86,87} Accordingly, they can be safely classified as class I quadrupolar dyes,¹⁹ the weak absorption solvatochromism being due to the V-shape of molecular geometry^{80,88}. With reference to dye **1** in Fig. 1, two transitions are observed in the visible range: the lowest-energy transition (at 2.54 eV in dichloromethane, DCM), corresponding to state *c*, is strongly allowed in 1PA, and has a weak 2PA intensity, while the second transition, at 3.22 eV in DCM, assigned to the *e*-state, is strongly 2PA-allowed and has a weak 1PA intensity. The proximity of the *c* and *e* state is another signature of class I dyes.

In curcumin-based ONPs, 1PA spectra are blueshifted (and broadened) compared to solution spectra, while in emission a sizeable redshift and a marked decrease of intensity is observed (similar effects are also observed in emission spectra of crystals). The spectral position of the 2PA band is marginally affected by aggregation, with a (weak) enhancement of intensity in ONP. The exciton picture qualitatively rationalizes the spectral behavior of aggregates of curcumin dyes: the blueshift of the absorption band and the strong decrease of fluorescence intensity are consistent with H-type aggregation, as observed for crystals.⁶³ Moreover, the exciton picture supports marginal aggregation effects on 2PA.

Table 1 compares experimental data for dye **1** in solution with TDDFT results (gas phase, crystallographic geometry, planar molecule; additional results can be found in the Supporting Information, Fig. S3-S4-S5 and Tables S1-S2). In agreement with experimental results, the lowest transition ($g \rightarrow c$) has a large oscillator strength, but a very weak 2PA cross section, while the second transition ($g \rightarrow e$) is marginally allowed in 1PA and has a strong 2PA activity (to compare absolute 2PA intensities, we notice that the Dalton results for σ_{2PA} refer to a linewidth $\Gamma = 0.1$ eV; accounting for the approximately three times larger experimental linewidth, would reduce the Dalton estimate of the 2PA intensity by a factor of 3). When compared with experiment, TDDFT transition energies are overestimated by ~ 0.8 eV. As expected, TDDFT results for solvated molecules (see SI, Table S2) reduce the discrepancy. Further improvement could be obtained accounting for molecular vibrations.⁸⁹ Our results are in agreement with a recent work about experimental and theoretical investigation of a family of curcumin dyes.⁸⁷

The $g \rightarrow c$ and $g \rightarrow e$ transitions, largely dominated by the $h \rightarrow l$ and $h \rightarrow l$ -1 configurations (h =monomer HOMO, l =monomer LUMO), have a clear *intramolecular* charge-transfer character, as shown by the frontier molecular orbitals in Fig. 3a, and can be readily identified with the $g \rightarrow c$ and $g \rightarrow e$ transitions of the ESM.

The experimental 1PA and 2PA energies fix the two parameters entering the electronic ESM Hamiltonian for **1** as $\eta = 0.94$ eV and $\tau = 0.93$ eV, corresponding to class I quadrupolar dye, with $\rho \sim 0.2$. The experimental molar extinction coefficient fixes $\mu_0 = 20$ D, that, in turns allow to estimate $\sigma_{2PA} \sim 1100$ GM ($\Gamma = 0.28$ eV). Accounting for screening effects (related to the squared refractive index) would reduce the ESMs estimate to ~ 500 GM, leading to a reasonable agreement with the experimental result.

Modelling curcumin aggregates

The crystal structure of **1** shows the presence of curcumin tetramers of the form T-P-P-T, where P and T represent two crystallographically inequivalent curcumin molecules, in a planar (P) and slightly twisted (T) geometry (see Fig. S3). Since TDDFT calculations are not viable for tetrameric structures, in order to validate the ESM approach, we discuss TDDFT results (same level of theory as for the monomer) on dimers at the crystallographic geometry, as well as at artificial geometries, where the intermolecular distance (r) is increased up to $\sim 9 \text{ \AA}$ in steps of 1 \AA .

Tables 2 and 3 summarize results from TDDFT calculations for curcumin P-P dimer at the crystallographic distance ($r = 3.74 \text{ \AA}$) and at the artificially augmented distance of 6.74 \AA . Results for other r values as well as for T-P dimers can be found in the SI. Fig. 3 shows relevant frontier orbitals together with their (approximate) relation to the frontier orbitals of the monomer (for the sake of clarity, we use lower-case letters, h and l , to refer to the molecular HOMO and LUMO, respectively, with index a and b referring to each one of the two molecules in the dimer, when relevant; we use capital H and L letters for the HOMO and LUMO of the dimer). As expected, each pair of equivalent molecular orbitals gives rise to two dimer orbitals that are basically degenerate at large distance and weakly interacting at the crystallographic geometry (the calculated splitting amounts to ~ 0.2 eV). As sketched in Fig. 3b, the $h \rightarrow l$ or c -transition of the monomer gives rise in the dimer to 4 transitions

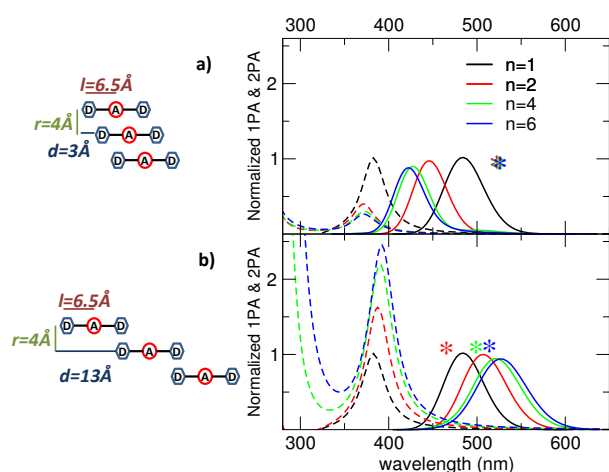


Fig. 5. Left panels: sketch of geometrical arrangements of aggregates of curcumins and geometrical parameters. Right panels: Calculated spectra for selected geometries of curcumin dimers. n is the number of molecules. Continuous and dashed lines refer to 1PA and 2PA spectra, respectively. The * marks the position of the lowest energy dark state (C_1). In order to compare the results obtained for systems of different dimensions, 1PA and 2PA intensities were divided by the number of molecules.

the aggregate. For comparison, the lower panels of Fig. 5 show results for a different geometry, where the relative lateral shift of the molecules amounts to 13 Å. In this case, corresponding to a J-aggregate, the bright 1PA state is redshifted with respect to the monomer, and, being the lowest excited state, supports good fluorescent properties for the aggregate.

ESM results in Fig. 5a are obtained for a geometry that mimics the experimental crystallographic geometry (most probably similar to the geometry in the ONPs) and, predicting H-type behavior, agree well with experimental data. Indeed experimental absorption spectra of organic nanoparticles are blueshifted with respect to the solvated dye and the fluorescence of both powders and nanoparticles is largely suppressed (the residual redshifted fluorescence observed in powders and nanoparticles can be ascribed to the activation of the dark state in Fig. 5a, due to molecular vibrations or to minor deviations from perfect alignment). Experimental 2PA of nanoparticles is marginally affected by intermolecular interactions. In agreement with the experiment, ESM results predict minor spectral shifts on 2PA bands

Squaraines: systems with high quadrupolar character

Squaraines are popular systems for nonlinear optical applications, particularly for their large 2PA cross section.^{38–45} Squaraines, characterized by a large mixing of the N and Z_+ states and by a marginal solvatochromism in absorption and in emission, belong to class II quadrupolar dyes. Their 1PA-active state, lying approximately at half the energy of the 2PA-active state, is responsible for a large (pre)resonance amplification of the 2PA intensity.^{19,42} The large mixing of the diabatic basis states makes squaraines strongly polarizable, so that important deviations from the exciton model are expected. As discussed in the literature, TDDFT does not offer reliable results for squaraines mainly due to

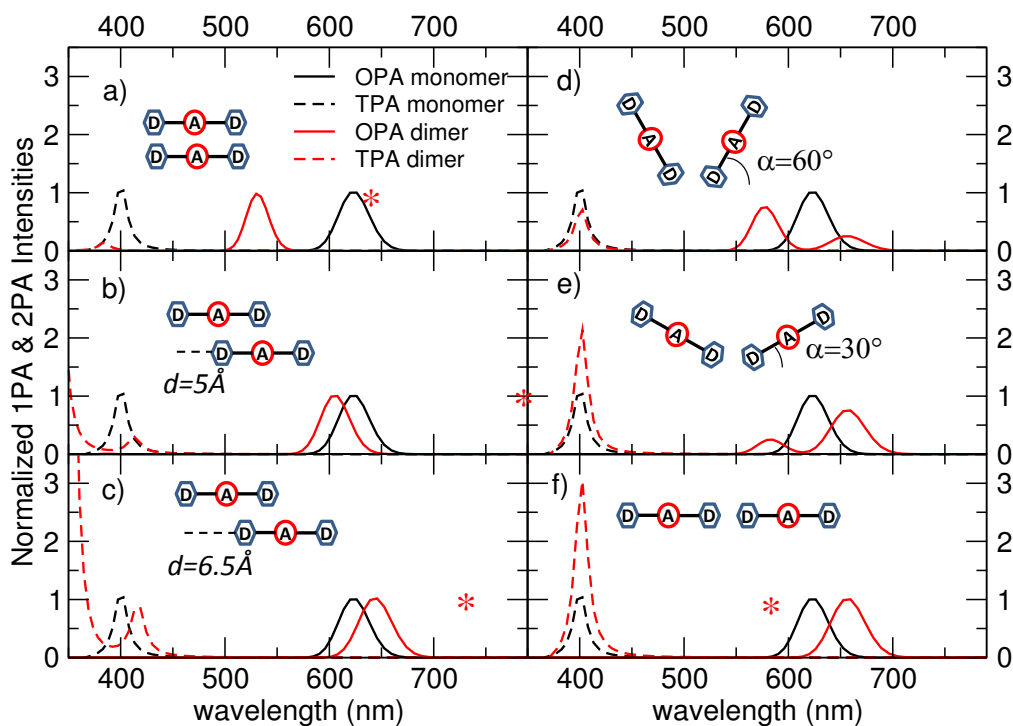


Fig. 6. Calculated spectra for selected geometries of dimers of squaraine 2. The * indicates the spectral position of the lowest dark c state (* is not shown in panels d and e, since both c-states are bright). ESM parameters: $\eta = 0.44$ eV and $\tau = 1.05$ eV. The length of the molecular arm is fixed to 5 Å. In left panels the distance between the two molecular axis is 5 Å. In right panels, the distance between the closest D groups is 5 Å.

the biradicaloid character of the dye.^{67–69} Therefore, we will not present TDDFT results for squaraine aggregates but will rely on ESMs. The resulting description of squaraines is somewhat oversimplified, but ESMs do not suffer from the drawback of TDDFT with biradicaloid and, while they do not account for localized excitations (including the excitations that involve the oxyallyl ring⁶⁷), they capture the basic physics of the low-energy transitions of squaraine dyes,^{19,80,81} offering a simple strategy to account for the subtle role of the molecular polarizability in aggregates.

We start our analysis with a rationalization of old results on squaraine dimers in controlled geometry.⁶⁶ Three different geometries are explored: a rigid dimer where a face-to-face arrangement is forced by a double bridge (CSq_mX); a series of dimers linked by a polymethylen spacer of increasing length (SqM_nSq, n=2–10) and a series of xylyl-bridged dimers (SqX_xSq, x = o-, m-, p-). CSq_mX shows a blueshifted band with respect to the monomer and is non-fluorescent, as expected for H-aggregates. In the SqM_nSq series, two absorption bands are observed, a blueshifted band with respect to the monomer and a more intense redshifted band (for n=10 a single band is observed, at the same energy as the monomer, suggesting negligible interchromophore interactions). A redshifted fluorescence is observed compared to the monomer, whose intensity is strongly suppressed for short spacers. A similar behavior is also observed for the SqX_xSq.

The observation of an intense redshifted absorption and a suppressed fluorescence, observed for both SqM_nSq and SqX_xSq series, is hard to rationalize in the exciton picture that, for aggregates showing a redshifted absorption, predicts also good fluorescent properties (J-aggregates). This strange result can be rationalized by ESMs, as shown by results in Fig. 6 (see also Fig. S16 in the SI). In ESMs, the isolated chromophore is parameterized against experimental data, setting $\eta = 0.44$ eV and $\tau = 1.05$ eV.⁸¹ In the faced geometry (Fig. 6a) as relevant to CSq_mX, the 1PA-active state of the monomers splits into a bright state to the blue and a dark state to the red, explaining the fully suppressed fluorescence for the dimer CSq_mX in Ref.⁶⁶ To describe SqM_nSq we can assume a “fan” geometry (Fig. 6d and 6e): in this case both exciton states originated from the c-state of the monomer are 1PA-active with relative intensities depending on the folding angle: for $\alpha < 45^\circ$ the redshifted state dominates the 1PA spectrum, while for $\alpha > 45^\circ$ the blueshifted state gives rise to a more intense transition, suggesting a suppression of fluorescence. Neither of the two cases is fully

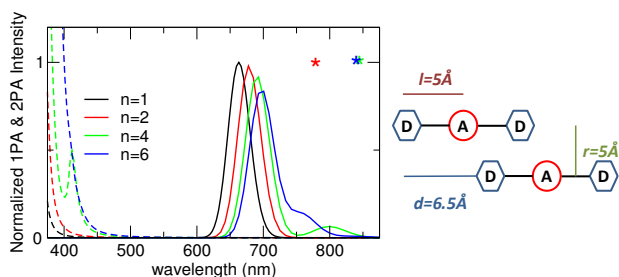


Fig. 7. Left panel: ESM calculation for aggregates of molecule **3** (parameters: $\eta = 0.064$ eV and $\tau = 1.2$ eV); n is the number of molecules. Continuous and dashed lines refer to one-photon and two-photon absorption spectra, respectively. The * refers to the lowest (in energy) dark state. The molecule was parameterized in the framework of ESM in Ref.⁸¹. Here we have renormalized the parameters to have the same quadrupolar character without accounting for molecular vibrations in a nonpolar solvent. Right panel: sketch of geometrical arrangements of aggregates and

consistent with experiment. For a ladder-geometry (Fig. 6c), ESM predicts instead an intense redshifted absorption band and at the same time a suppression of fluorescence due to the presence of a dark state further to the red. In this case, however, the model does not predict any blueshifted absorption band. To rationalize experimental data we suggest that in solution geometries as in Fig. 6c and 6e do coexist.

Xylyl-bridged dimers, SqX_xSq, show two 1PA bands to the red and to the blue of the monomer absorption and a similar fluorescence quantum yield as the monomer. The highest fluorescence quantum yield is observed in SqX_pSq, where the two chromophores are in *para* position, and it decreases of a factor of 1.5 and 2.5 in SqX_mSq (*meta*) and SqX_oSq (*ortho*). Based on available experimental data, SqX_pSq, SqX_mSq and SqX_oSq can be described by the geometrical arrangement in Fig. 6f, 6e and 6d respectively. For SqX_pSq, the second absorption band is dark in calculation, but it can acquire some intensity introducing molecular vibrations or interaction with the solvent.

In a recent paper, Belfield and coworkers investigate squaraine aggregates in water, observing a blue-shifted absorption and a strong decrease of fluorescence intensity, supporting the formation of H-aggregates.⁴⁰ The addition of a polyelectrolyte to the solution of the (cationic) squaraine leads to a strong redshifted absorption and to a complete suppression of fluorescence, a phenomenon ascribed to the formation of a “non-fluorescent J-aggregate”.⁴⁰ The 2PA signal of the monomer and H-aggregate is negligible in the 400–500nm region, while an intense 2PA absorption (~460 GM) is observed in the presence of the polyelectrolyte (unfortunately the full shape of the 2PA band is not experimentally accessible due to resonance effects). The two observations of suppressed fluorescence in J-aggregates and of sizable effects on 2PA both contrast sharply with the exciton picture, but are naturally rationalized within ESM. For the squaraines investigated in ref.⁴⁰ (molecule **3** in Fig. 1) we set up the molecular model fixing $\eta = 0.164$ eV and $\tau = 1.2$ eV. Fig. 7 shows 1PA and 2PA spectra calculated for a ladder geometry with a large lateral shift (6.5 Å). Similarly to results shown in Fig. 6c, in this geometry both dimer states originated from the 1PA-active monomer states are redshifted with respect to the monomer and the lowest-energy state is a dark state. For this geometry, we then expect a strong suppression of the fluorescence (as for an H-aggregate) even if the observed absorption is redshifted (as for a J-aggregate). The reason for this anomalous behavior is in the large polarizability of squaraines: because of the electrostatic interaction with the surrounding molecules, a squaraine molecule readjusts its charge distribution, leading to a variation of the transition frequency of each chromophore in the aggregate. For the aggregate in Fig. 7 we calculate the absorption spectrum in the mean-field approximation for a molecule experiencing the electric field generated by surrounding molecules (see Fig. S17) and obtain a very large redshift of the absorption band with respect to the gas-phase monomer. The exciton splitting with respect to the mean-field absorption would then lead to a blueshifted intense absorption and a redshifted dark state, as in a classical H-aggregate, even if, when compared to the isolated dye, both transitions are redshifted. ESMs then provide a simple interpretation for the puzzling experimental observation of *non-fluorescent J-aggregates* in ref.⁴⁰: the redshifted absorption band in

the aggregate is not due to the lowest energy state in the exciton band (as found in traditional fluorescent J-aggregates), it is rather due to the highest energy state in the exciton band (as in traditional non-fluorescent H-aggregates). The observed red-shift is ascribed in these conditions to an overall red-shift of the whole exciton band with respect to the isolated molecule due to mean field effects, that are very strong in aggregates of largely polarizable dyes like squaraines. In this context, the definition of J- and H-aggregates becomes hardly applicable when referred to highly polarizable molecules, as already pointed out in ref.²⁵ Our results also agree with experimental 2PA data: indeed, according to Fig. 7, the 2PA cross section is negligible in the 400–500nm spectral region for the monomer and dimer, but it increases for big aggregates.

Conclusions

The extensive analysis of experimental results on several families of aggregates of quadrupolar dyes, also supported by TDDFT results on dimeric structures, gives confidence about the possibility to reliably model and rationalize the properties of molecular aggregates fully accounting for the molecular polarizability and relaxing the dipolar approximation. ESMs fairly naturally lend themselves to this aim, offering a versatile alternative to the exciton model to deal with large molecular aggregates.

Quadrupolar dyes are of special interest for 2PA applications, and controlling aggregation phenomena in quadrupolar-based aggregates and/or ONPs has a potential big impact for two-photon microscopy applications. In this respect, it is of paramount importance to understand aggregation effects on both 2PA spectra and on the fluorescence quantum yield: the two-photon brilliance as relevant to microscopy applications is in fact defined as the product of the 2PA intensity times the fluorescence quantum yield. According to our results, for one-dimensional structures, the 2PA intensity can be amplified considerably if quadrupolar dyes are set in an aligned geometry or, at least, in a face-to-face geometry with a large lateral shift (ladder geometry). Quite interestingly, the aligned geometry shall also lead to brightly fluorescent aggregates, while in the ladder geometry we expect a suppressed fluorescence. An amplification of the 2PA response while maintaining good fluorescence properties can be obtained in a two-dimensional brickwork arrangement, as reported in Ref.⁹⁰. In this paper, authors demonstrate the formation of strongly fluorescent J-aggregates of quadrupolar dyes and the concomitant amplification of the 2PA cross section. Preliminary results on 2D structures are reported in supporting information (Fig. S18): results are promising and in agreement with experimental data. The investigation of brickwork structures deserves more attention, in order to thoroughly understand the relationship between structure and properties, and will be the subject of future work.

The recurrent observation of *non-fluorescent J-aggregates* of squaraines or, to be more precise, aggregates where, in spite of a redshifted absorption, the fluorescence is strongly suppressed, calls for explanations well beyond the exciton model. Recently, this behavior has been ascribed to the effect of important intermolecular CT interactions,²⁵ and for sure this is a possibility in some systems. However, even in the absence of intermolecular CT interactions, ESMs support non-fluorescent J-aggregates due to the

large polarizability of squaraine molecules. In aggregates of highly polarizable molecules, not only the exciton model becomes hardly applicable, but the very same definition of J- and H-aggregates becomes misleading.

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Notes and references

- 1 J. R. Lakowicz, Ed., *Principles of Fluorescence Spectroscopy*, Springer US, Boston, MA, 2006.
- 2 B. Valeur, *Molecular Fluorescence*, Wiley-VCH Verlag GmbH, Weinheim, FRG, 2001.
- 3 T. Renger, *Photosynth. Res.*, 2009, **102**, 471–485.
- 4 A. S. Davydov, *Theory of Molecular Excitons*, New York, Plenum Pres., 1971.
- 5 V. M. Agranovich and M. D. Galanin, 1982, **3909**, 371.
- 6 T. Förster, *Ann. Phys.*, 1948, **437**, 55–75.
- 7 T. Förster, in *Modern quantum chemistry*, Academic p., 1965, p. 93.
- 8 K. Mukai, S. Abe and H. Sumi, *J. Phys. Chem. B*, 1999, **103**, 6096–6102.
- 9 K. F. Wong, B. Bagchi and P. J. Rossky, *J. Phys. Chem. A*, 2004, **108**, 5752–5763.
- 10 T. I. Hukka, T. Toivonen, E. Hennebicq, J.-L. Brédas, R. A. J. Janssen and D. Beljonne, *Adv. Mater.*, 2006, **18**, 1301–1306.
- 11 D. Beljonne, C. Curutchet, G. D. Scholes and R. J. Silbey, *J. Phys. Chem. B*, 2009, **113**, 6583–6599.
- 12 C. Sissa, A. K. Manna, F. Terenziani, A. Painelli and S. K. Pati, *Phys. Chem. Chem. Phys.*, 2011, **13**, 12734–12744.
- 13 F. Terenziani, G. D'Avino and A. Painelli, *ChemPhysChem*, 2007, **8**, 2433–2444.
- 14 G. D'Avino, F. Terenziani and A. Painelli, *J. Phys. Chem. B*, 2006, **110**, 25590–25592.
- 15 A. Painelli and F. Terenziani, *J. Am. Chem. Soc.*, 2003, **125**, 5624–5625.
- 16 F. Terenziani and A. Painelli, *Phys. Rev. B*, 2003, **68**, 165405.
- 17 A. Painelli, *Chem. Phys. Lett.*, 1998, **285**, 352–358.
- 18 A. Painelli and F. Terenziani, *Chem. Phys. Lett.*, 1999, **312**, 211–220.
- 19 F. Terenziani, A. Painelli, C. Katan, M. Charlot and M. Blanchard-Desce, *J. Am. Chem. Soc.*, 2006, **128**, 15742–15755.
- 20 F. Terenziani, C. Sissa and A. Painelli, *J. Phys. Chem. B*, 2008, **112**, 5079–5087.
- 21 L. Grisanti, C. Sissa, F. Terenziani, A. Painelli, D. Roberto, F. Tessore, R. Ugo, S. Quici, I. Fortunati, E. Garbin, C. Ferrante

- and R. Bozio, *Phys. Chem. Chem. Phys.*, 2009, **11**, 9450–9457.
- 22 J. Campo, A. Painelli, F. Terenziani, T. Van Regemorter, D. Beljonne, E. Goovaerts and W. Wenseleers, *J. Am. Chem. Soc.*, 2010, **132**, 16467–16478.
- 23 S. A. Kurhuzenkau, A. W. Woodward, S. Yao, K. D. Belfield, Y. O. Shaydyuk, C. Sissa, M. V. Bondar and A. Painelli, *Phys. Chem. Chem. Phys.*, 2016, **18**, 12839–12846.
- 24 C. Sissa, V. Calabrese, M. Cavazzini, L. Grisanti, F. Terenziani, S. Quici and A. Painelli, *Chem. - A Eur. J.*, 2013, **19**, 924–935.
- 25 N. J. Hestand, C. Zheng, A. R. Penmetcha, B. Cona, J. A. Cody, F. C. Spano and C. J. Collison, *J. Phys. Chem. C*, 2015, **119**, 18964–18974.
- 26 C. Sissa, F. Terenziani, A. Painelli, A. K. Manna and S. K. Pati, *Chem. Phys.*, 2012, **404**, 9–15.
- 27 C. Sissa, F. Terenziani, A. Painelli, A. Abboto, L. Bellotto, C. Marinzi, E. Garbin, C. Ferrante and R. Bozio, *J. Phys. Chem. B*, 2010, **114**, 882–893.
- 28 F. Todescato, I. Fortunati, S. Carlotto, C. Ferrante, L. Grisanti, C. Sissa, A. Painelli, A. Colombo, C. Dragonetti and D. Roberto, *Phys. Chem. Chem. Phys.*, 2011, **13**, 11099–109.
- 29 A. Painelli, F. Terenziani, L. Angiolini, T. Benelli and L. Giorgini, *Chem. - A Eur. J.*, 2005, **11**, 6053–6063.
- 30 F. Terenziani, M. Morone, S. Gmouh and M. Blanchard-Desce, *ChemPhysChem*, 2006, **7**, 685–696.
- 31 F. Terenziani, O. Mongin, C. Katan, B. K. G. Bhatthula and M. Blanchard-Desce, *Chem. - A Eur. J.*, 2006, **12**, 3089–3102.
- 32 F. Terenziani, S. Ghosh, A.-C. Robin, P. K. Das and M. Blanchard-Desce, *J. Phys. Chem. B*, 2008, **112**, 11498–11505.
- 33 F. Terenziani, V. Parthasarathy, A. Pla-Quintana, T. Maishal, A. M. Caminade, J. P. Majoral and M. Blanchard-Desce, *Angew. Chemie - Int. Ed.*, 2009, **48**, 8691–8694.
- 34 V. Parthasarathy, R. Pandey, F. Terenziani, P. K. Das and M. Blanchard-Desce, *Phys. Chem. Chem. Phys.*, 2014, **16**, 9096.
- 35 G. D'Avino, L. Grisanti, J. Guasch, I. Ratera, J. Veciana and A. Painelli, *J. Am. Chem. Soc.*, 2008, **130**, 12064–12072.
- 36 G. D'Avino, L. Grisanti, A. Painelli, J. Guasch, I. Ratera and J. Veciana, *CrystEngComm*, 2009, **11**, 2040.
- 37 J. Guasch, L. Grisanti, S. Jung, D. Morales, G. D'Avino, M. Souto, X. Fontrodona, A. Painelli, F. Renz, I. Ratera and J. Veciana, *Chem. Mater.*, 2013, **25**, 808–814.
- 38 S. Sreejith, P. Carol, P. Chithra and A. Ajayaghosh, *J. Mater. Chem.*, 2008, **18**, 264–274.
- 39 L. Beverina and P. Salice, *Eur. J. Org. Chem.*, 2010, 1207.
- 40 Y. Zhang, B. Kim, S. Yao, M. V. Bondar and K. D. Belfield, *Langmuir*, 2013, **29**, 11005–11012.
- 41 H.-Y. Ahn, S. Yao, X. Wang and K. D. Belfield, *ACS Appl. Mater. Interfaces*, 2012, **4**, 2847–2854.
- 42 J. Fu, L. A. Padilha, D. J. Hagan, E. W. Van Stryland, O. V. Przhonska, M. V. Bondar, Y. L. Slominsky and A. D. Kachkovski, *J. Opt. Soc. Am. B*, 2007, **24**, 67.
- 43 S. Webster, J. Fu, L. A. Padilha, O. V. Przhonska, D. J. Hagan, E. W. Van Stryland, M. V. Bondar, Y. L. Slominsky and A. D. Kachkovski, *Chem. Phys.*, 2008, **348**, 143–151.
- 44 D. Scherer, R. Dörfler, A. Feldner, T. Vogtmann, M. Schwoerer, U. Lawrentz, W. Grahn and C. Lambert, *Chem. Phys.*, 2002, **279**, 179–207.
- 45 S. Ohira, I. Rudra, K. Schmidt, S. Barlow, S.-J. Chung, Q. Zhang, J. Matichak, S. R. Marder and J.-L. Brédas, *Chem. - A Eur. J.*, 2008, **14**, 11082–11091.
- 46 J. Daniel, A. G. Godin, M. Palayret, B. Lounis, L. Cognet and M. Blanchard-Desce, *J. Phys. D. Appl. Phys.*, 2016, **49**, 084002.
- 47 J. M. Hales, D. J. Hagan, E. W. Van Stryland, K. J. Schafer, A. R. Morales, K. D. Belfield, P. Pacher, O. Kwon, E. Zojer and J. L. Bredas, *J. Chem. Phys.*, 2004, **121**, 3152–3160.
- 48 C. D. Andrade, C. O. Yanez, L. Rodriguez and K. D. Belfield, *J. Org. Chem.*, 2010, **75**, 3975–3982.
- 49 C. Rouxel, M. Charlot, Y. Mir, C. Frochet, O. Mongin and M. Blanchard-Desce, *New J. Chem.*, 2011, **35**, 1771.
- 50 O. Mongin, L. Porrès, M. Charlot, C. Katan and M. Blanchard-Desce, *Chem. - A Eur. J.*, 2007, **13**, 1481–1498.
- 51 M. Charlot, N. Izard, O. Mongin, D. Riehl and M. Blanchard-Desce, *Chem. Phys. Lett.*, 2006, **417**, 297–302.
- 52 H. Y. Woo, B. Liu, B. Kohler, D. Korystov, A. Mikhailovsky and G. C. Bazan, *J. Am. Chem. Soc.*, 2005, **127**, 14721–14729.
- 53 S. J. K. Pond, M. Rumi, M. D. Levin, T. C. Parker, D. Beljonne, M. W. Day, J.-L. Brédas, S. R. Marder and J. W. Perry, *J. Phys. Chem. A*, 2002, **106**, 11470–11480.
- 54 B. Strehmel, A. M. Sarker and H. Detert, *ChemPhysChem*, 2003, **4**, 249–259.
- 55 Y. Tian, C.-Y. Chen, Y.-J. Cheng, A. C. Young, N. M. Tucker and A. K.-Y. Jen, *Adv. Funct. Mater.*, 2007, **17**, 1691–1697.
- 56 M. Montalti, L. Prodi, E. Rampazzo and N. Zaccheroni, *Chem. Soc. Rev.*, 2014, **43**, 4243.
- 57 T. O. McDonald, P. Martin, J. P. Patterson, D. Smith, M. Giardiello, M. Marcello, V. See, R. K. O'Reilly, A. Owen and S. Rannard, *Adv. Funct. Mater.*, 2012, **22**, 2469–2478.
- 58 V. Parthasarathy, S. Fery-Forgues, E. Campioli, G. Recher, F. Terenziani and M. Blanchard-Desce, *Small*, 2011, **7**, 3219–3229.
- 59 E. Campioli, C. Rouxel, M. Campanini, L. Nasi, M. Blanchard-Desce and F. Terenziani, *Small*, 2013, **9**, 1982–1988.
- 60 E. Campioli, D. M. Nikolaidou, V. Hugues, M. Campanini, L. Nasi, M. Blanchard-Desce and F. Terenziani, *J. Mater. Chem. C*, 2015, **3**, 7483–7491.
- 61 D. Horn and J. Rieger, *Angew. Chemie Int. Ed.*, 2001, **40**, 4330.
- 62 J. Zhang, R. Chen, Z. Zhu, C. Adachi, X. Zhang and C.-S. Lee, *ACS Appl. Mater. Interfaces*, 2015, **7**, 26266–26274.
- 63 A. D'Aléo, A. Felouat, V. Heresanu, A. Ranguis, D. Chaudanson, A. Karapetyan, M. Giorgi and F. Fages, *J. Mater. Chem. C*, 2014, **2**, 5208–5215.
- 64 L. Aparicio-Ixta, M. Rodriguez and G. Ramos-Ortiz, in *Contemporary Optoelectronics*, 2016, pp. 25–50.
- 65 J. Rodríguez-Romero, L. Aparicio-Ixta, M. Rodríguez, G. Ramos-Ortiz, J. L. Maldonado, A. Jiménez-Sánchez, N. Farfán and R. Santillan, *Dye. Pigment.*, 2013, **98**, 31–41.

- 66 K. Liang, M. S. Farahat, J. Perlstein, K.-Y. Law and D. G. Whitten, *J. Am. Chem. Soc.*, 1997, **119**, 830–831.
- 67 K. Srinivas, C. Prabhakar, C. Lavanya Devi, K. Yesudas, K. Bhanuprakash and V. Jayathirtha Rao, *J. Phys. Chem. A*, 2007, **111**, 3378–3386.
- 68 G. Krishna Chaitanya, A. L. Puyad and K. Bhanuprakash, *RSC Adv.*, 2015, **5**, 18813–18821.
- 69 J. Fabian, *Dye. Pigment.*, 2010, **84**, 36–53.
- 70 M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, B. Mennucci, G. A. Petersson, H. Nakatsuji, M. Caricato, X. Li, H. P. Hratchian, A. F. Izmaylov, J. Bloino, G. Zheng, J. L. Sonnenberg, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, J. Montgomery, J. A., J. E. Peralta, F. Ogliaro, M. Bearpark, J. J. Heyd, E. Brothers, K. N. Kudin, V. N. Staroverov, R. Kobayashi, J. Normand, K. Raghavachari, A. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, N. Rega, J. M. Millam, M. Klene, J. E. Knox, J. B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, R. L. Martin, K. Morokuma, V. G. Zakrzewski, G. A. Voth, P. Salvador, J. J. Dannenberg, S. Dapprich, A. D. Daniels, Ö. Farkas, J. B. Foresman, J. V. Ortiz, J. Cioslowski and D. J. Fox, 2009, Gaussian Inc. Wallingford CT.
- 71 A. D. Becke, *Phys. Rev. A*, 1988, **38**, 3098–3100.
- 72 J.-D. Chai and M. Head-Gordon, *Phys. Chem. Chem. Phys.*, 2008, **10**, 6615.
- 73 J. Tomasi, B. Mennucci and R. Cammi, *Chem. Rev.*, 2005, **105**, 2999–3094.
- 74 T. Yanai, D. P. Tew and N. C. Handy, *Chem. Phys. Lett.*, 2004, **393**, 51–57.
- 75 K. Aidas, C. Angeli, K. L. Bak, V. Bakken, R. Bast, L. Boman, O. Christiansen, R. Cimiraglia, S. Coriani, P. Dahle, E. K. Dalskov, U. Ekström, T. Enevoldsen, J. J. Eriksen, P. Ettenhuber, B. Fernández, L. Ferrighi, H. Fliegl, L. Frediani, K. Hald, A. Halkier, C. Hättig, H. Heiberg, T. Helgaker, A. C. Hennum, H. Hettema, E. Hjertenaes, S. Høst, I.-M. Høyvik, M. F. Iozzi, B. Jansík, H. J. A. Jensen, D. Jonsson, P. Jørgensen, J. Kauczor, S. Kirpekar, T. Kjaergaard, W. Klopper, S. Knecht, R. Kobayashi, H. Koch, J. Kongsted, A. Krapp, K. Kristensen, A. Ligabue, O. B. Lutnaes, J. I. Melo, K. V. Mikkelsen, R. H. Myhre, C. Neiss, C. B. Nielsen, P. Norman, J. Olsen, J. M. H. Olsen, A. Osted, M. J. Packer, F. Pawłowski, T. B. Pedersen, P. F. Provasi, S. Reine, Z. Rinkevicius, T. A. Ruden, K. Ruud, V. V. Rybkin, P. Sałek, C. M. Samson, A. S. de Merás, T. Saue, S. P. A. Sauer, B. Schimmelpfennig, K. Sneskov, A. H. Steindal, K. O. Sylvester-Hvid, P. R. Taylor, A. M. Teale, E. I. Tellgren, D. P. Tew, A. J. Thorvaldsen, L. Thøgersen, O. Vahtras, M. A. Watson, D. J. D. Wilson, M. Ziolkowski and H. Ågren, *Wiley Interdiscip. Rev. Comput. Mol. Sci.*, 2014, **4**, 269–284.
- 76 P. R. Monson, *J. Chem. Phys.*, 1970, **53**, 29.
- 77 C.-K. Wang, K. Zhao, Y. Su, Y. Ren, X. Zhao and Y. Luo, *J. Chem. Phys.*, 2003, **119**, 1208.
- 78 M. Sun, J. Chen and H. Xu, *J. Chem. Phys.*, 2008, **128**, 064106.
- 79 F. Terenziani, O. V. Przhonska, S. Webster, L. A. Padilha, Y. L. Slominsky, I. G. Davydenko, A. O. Gerasov, Y. P. Kovtun, M. P. Shandura, A. D. Kachkovski, D. J. Hagan, E. W. Van Stryland and A. Painelli, *J. Phys. Chem. Lett.*, 2010, **1**, 1800–1804.
- 80 C. Sissa, F. Terenziani, A. Painelli, R. B. K. Siram and S. Patil, *J. Phys. Chem. B*, 2012, **116**, 4959–4966.
- 81 K. M. Shafeekh, S. Das, C. Sissa and A. Painelli, *J. Phys. Chem. B*, 2013, **117**, 8536–8546.
- 82 H. Hu, O. V. Przhonska, F. Terenziani, A. Painelli, D. Fishman, T. R. Ensley, M. Reichert, S. Webster, J. L. Bricks, A. D. Kachkovski, D. J. Hagan and E. W. Van Stryland, *Phys. Chem. Chem. Phys.*, 2013, **15**, 7666.
- 83 C. Sissa, P. M. Jahani, Z. G. Soos and A. Painelli, *ChemPhysChem*, 2012, **13**, 2795–2800.
- 84 B. J. Orr and J. F. Ward, *Mol. Phys.*, 1971, **20**, 513–526.
- 85 C. Sissa, V. Parthasarathy, D. Drouin-Kucma, M. H. V Werts, M. Blanchard-Desce and F. Terenziani, *Phys. Chem. Chem. Phys.*, 2010, **12**, 11715–11727.
- 86 A. Felouat, A. D'Aléo and F. Fages, *J. Org. Chem.*, 2013, **78**, 4446–4455.
- 87 K. Kamada, T. Namikawa, S. Senatore, C. Matthews, P.-F. Lenne, O. Maury, C. Andraud, M. Ponce-Vargas, B. Le Guennic, D. Jacquemin, P. Agbo, D. D. An, S. S. Gaunay, X. Liu, R. J. Abergel, F. Fages and A. D'Aléo, *Chem. - A Eur. J.*, 2016, **22**, 5219–5232.
- 88 G. Ponterini, D. Vanossi, Z. A. Krasnaya, A. S. Tatikolov and F. Momicchioli, *Phys. Chem. Chem. Phys.*, 2011, **13**, 9507.
- 89 F. Santoro, R. Improta, A. Lami, J. Bloino and V. Barone, *J. Chem. Phys.*, 2007, **126**, 084509.
- 90 Z. Xu, Q. Liao, Y. Wu, W. Ren, W. Li, L. Liu, S. Wang, Z. Gu, H. Zhang and H. Fu, *J. Mater. Chem.*, 2012, **22**, 17737.