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# 1 Remarks on the room temperature impurity band conduction in heavily 2 Al<sup>+</sup> implanted 4H-SiC

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10 The processing parameters which favour the onset of an impurity band conduction around room  
11 temperature with a contemporaneous elevated p-type conductivity in Al<sup>+</sup> implanted 4H-SiC are  
12 highlighted by comparing original and literature results. In the examined cases, Al is implanted at  
13 300–400 °C, in concentrations from below to above the Al solubility limit in 4H-SiC  
14 ( $2 \times 10^{20} \text{ cm}^{-3}$ ) and post implantation annealing temperature is  $\geq 1950$  °C. Transport measurements  
15 feature the onset of an impurity band conduction, appearing at increasing temperature for increas-  
16 ing Al implant dose, until this transport mechanism is enabled around room temperature. This condi-  
17 tion appears suitable to guarantee a thermal stability of the electrical properties. In this study, the  
18 heaviest doped and less resistive samples (Al implanted concentration of  $5 \times 10^{20} \text{ cm}^{-3}$  and resistiv-  
19 ity of about  $2 \times 10^{-2} \Omega \text{ cm}$ ) show a carrier density above the Al solubility limit, which is consis-  
20 tent with at least a 50% electrical activation for a 15% compensation. The model of Miller and  
21 Abrahams well describes the resistivity data of the lower doped sample, whereas a deviation from  
22 the behaviour predicted by such a model is observed in the higher doped specimens, consistent  
23 with the occurrence of a variable range hopping at low temperature. © 2015 AIP Publishing LLC.

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## 24 INTRODUCTION

25 Ion implantation is the most used technology for obtain-  
26 ing planar selective area doping and impurity doping concen-  
27 tration far above the solid solubility limit in semiconductor  
28 materials for electronic device applications and for funda-  
29 mental studies. Aluminum (Al) is the preferred acceptor dop-  
30 ing species in SiC when very low p-type resistivity values  
31 are desired. To the best of the authors' knowledge, and only  
32 for demonstration purposes, the maximum implanted Al con-  
33 centration in the p-type emitters of SiC p-i-n diodes has been  
34  $1.5 \times 10^{20} \text{ cm}^{-3}$ , see, for example, Refs. 1–3. In general, an  
35 increase of the semiconductor doping is desired in the device  
36 contact areas for reducing the contact resistance.

37 The state of the art on the electrical activation of implanted  
38 Al in 4H-SiC is hereafter resumed. For a given implanted Al  
39 concentration, the p-type doping increases with the increase of  
40 the post implantation annealing temperature, while for a fixed  
41 post implantation annealing temperature, the p-type doping  
42 increases with increasing implanted Al concentration.  
43 Maximum doping values have been obtained for 1950–2100 °C  
44 annealing with conventional<sup>4,5</sup> and microwave heating.<sup>2,3</sup>  
45 Minimum room temperature (RT) resistivity values of few  $10^{-2}$   
46  $\Omega \text{ cm}$ , which are good for sheet resistance values  $< 10^4 \Omega/\square$ ,  
47 have been obtained by implanted Al concentrations above the  
48 solubility limit of  $2 \times 10^{20} \text{ cm}^{-3}$ ,<sup>6</sup> and post implantation anneal-  
49 ing temperatures  $\geq 1950$  °C.<sup>4,5,7</sup> The characterization of the hole  
50 transport in such low p-type resistivity Al implanted 4H-SiC  
51 materials allow us to hypothesize that implanted Al concentra-  
52 tions above  $1.5 \times 10^{20} \text{ cm}^{-3}$  could be used for the fabrication of  
53 highly conductive p-type paths in high temperature SiC sensors,

or for designing new current collection geometries in SiC power 54  
55 devices. In fact, the temperature dependence of the p-type resistiv-  
56 ity in such SiC materials features a weak temperature depend-  
57 ence associated to the formation of an impurity band (IB)  
58 conduction around room temperature,<sup>2–4,8,9</sup> which guarantee p-  
59 type SiC materials of almost stable transport features in a wide  
60 large temperature range around RT. It is worthwhile to remem-  
61 ber that for dopant concentration below the  $10^{20} \text{ cm}^{-3}$  decade,  
62 the high thermal ionization energy of every dopant species in  
63 SiC is responsible of a strong temperature dependence of the  
64 SiC transport properties due to carrier freeze-out effects, see, for  
65 example, Refs. 10 and 11.

66 The aim of this article is to highlight the identification of the  
67 processing parameters which favour the onset of an impurity  
68 band conduction around room temperature joined to an elevated  
69 p-type conductivity in Al<sup>+</sup> implanted 4H-SiC. Both original and  
70 literature data are used for this purpose. Moreover, details on the  
71 transport data that support the identification of the IB transport  
72 mechanism in samples of different Al implant concentrations are  
73 discussed, by claiming the role of such a mechanism in obtaining  
74 very low resistivity values and a carrier density that are nearly  
75 temperature independent around RT. For one of the heavier  
76 doped samples, the consistency of the low temperature conduc-  
77 tivity data with the Mott law was evidenced, suggesting the onset  
78 of a variable range hopping transport at low temperature.

## 79 SAMPLE PROCESSING AND MEASUREMENTS

80 The discussion of the transport properties of Al<sup>+</sup> heavily  
81 implanted 4H-SiC samples takes off from two widely recog-  
82 nized observations: (i) the increase of the post implantation

annealing temperature leads to a more efficient electrical activation of the implanted Al impurities<sup>2,4,8</sup> and (ii) the increase of the activated Al concentration shifts towards higher temperatures, the onset of a hole conduction through impurity states.<sup>8,10</sup>

This work, following the result (i), takes into account only samples annealed at the maximum reachable temperatures of 1950 °C and 2000 °C by an inductively heated furnace<sup>4</sup> and by microwave heating,<sup>7</sup> respectively. Moreover, to discuss benefit effects of the result (ii), samples of implant concentration above  $1 \times 10^{20} \text{ cm}^{-3}$  are accounted for, in the range  $1.5 \times 10^{20} - 5 \times 10^{20} \text{ cm}^{-3}$ . In fact, samples with Al implanted concentration below  $1 \times 10^{20} \text{ cm}^{-3}$ , although submitted to the 1950 °C–2000 °C thermal treatments, exhibit a significant carrier freeze-out into impurities in a wide range of temperatures, where an electrical transport in valence band states (VB) is recognizable.<sup>10</sup> Features of an IB transport appear, in these samples, only by decreasing enough the temperature of measurement. The use of implanted Al concentrations above  $1 \times 10^{20} \text{ cm}^{-3}$  and 1950 °C–2000 °C annealing has the effect to enhance the acceptor density, to shift the onset of the impurity band conduction towards RT and to avoid a temperature region dominated by carrier freeze-out. This condition has been effectively seen for Al implanted concentrations  $\geq 3 \times 10^{20} \text{ cm}^{-3}$ .<sup>4</sup> It is worthwhile to notice that such a density is higher than the Al solubility limit in 4H-SiC at 2000 °C,  $2 \times 10^{20} \text{ cm}^{-3}$ .<sup>6</sup>

The samples here investigated are in part a selection from previous studies and in part new processed specimens, all that with the purpose to obtain an homogeneous set of identical Al<sup>+</sup> implanted 4H-SiC with 1950 °C–2000 °C post implantation annealing obtained by the two mentioned heating methods, conventional and microwave. Possible effects of different implant temperatures 300 °C and 400 °C were also inquired. Table I summarizes the sample set of this study together with their processing parameters, which are detailed in the following.

High purity semi-insulating, 8° off-axis (0001) 4H-SiC wafers were Al<sup>+</sup> implanted with different energy and dose values to obtain almost box shaped Al depth profiles next to the wafer surface. A Tandemtron 1.7 MV accelerator (High Voltage Engineering Europa B.V.) and 3 inches hot holder for sample mounting and heating were used. During implantation, the SiC samples were covered by a thick SiO<sub>2</sub> film

and kept at 300 °C or at 400 °C. More precisely, samples used for previous studies were implanted at 400 °C, while the original samples of this study have been implanted at 300 °C. Implantation schedules were decided by using SRIM2008 simulations<sup>12</sup> and verified by Secondary Ion Mass Spectroscopy (SIMS) on few samples. Homogeneous Al concentrations of  $1.5 \times 10^{20}$ ,  $3 \times 10^{20}$ , and  $5 \times 10^{20} \text{ cm}^{-3}$  were obtained across a thickness of about 400 nm. The implanted wafers were diced into pieces of 5 mm × 5 mm for facilitating van der Pauw (vdP) Hall measurements. These pieces were annealed at 1950 °C/5 min in a conventional inductively heated furnace (“conventional annealing” CA) or at 2000 °C/30 s in a microwave heating system (“microwave annealing” MWA). Details about these CA and MWA systems and their characteristic temperature versus time cycles are provided in Refs. 2, 7, 13, and 14. During CA and MWA, the implanted sample surface was protected by a carbon film (C-cap), which was obtained by a 900 °C/2 min pyrolysis in forming gas of a 2–4 μm thick resist film.<sup>15</sup> Before the spinning of the resist film, the SiC native oxide was etched away in a hydrofluoric acid bath and samples were dried in nitrogen at 110 °C for 30 min. After CA and MWA, C-cap was removed by 850 °C/15 min dry oxidation. Root mean square (rms) surface roughness after C-cap removal was measured by Atomic Force Microscopy in the tapping mode on a few samples and found to be in the range of 0.5–4.7 nm.<sup>5</sup>

It is widely accepted that the implanted Al does not diffuse during post implantation annealing.<sup>9,16</sup> This has been assumed true for all the samples of this study, which is an approximation. Such an approximation is corroborated by the fact that the measured Hall hole density always increases with the implanted Al concentration, even when this latter increases above the solubility value. Moreover, Hall hole densities overcoming the Al solubility value are effectively measured as it was shown in previous reports<sup>2–5</sup> and will be recalled here in the “Results and Discussion” section.

Square van der Pauw (vdP) devices have been obtained by fabricating triangular ohmic contacts on the four corners of each 5 mm × 5 mm annealed samples. For ohmic contacts, sputtered Ti(80 nm)/Al(2% Si, 350 nm) films alloyed at 1000 °C for 2 min in vacuum have been used. Due to the non-negligible dimensions of the contacts compared to the device size, correction factors have been applied to the results of electrical measurements as suggested in Ref. 17. In

TABLE I. Process parameters of the Al<sup>+</sup> implanted p-type 4H-SiC samples of this study. From left to right, the column content is: sample label with, if the case, citation of previous articles where the same sample has been used, simulated implanted Al concentration by SRIM2008,<sup>12</sup> implantation temperature, measured as-implanted Al concentration by SIMS, post implantation annealing type (CA and MWA) with temperature and time, RT Hall hole density, and RT resistivity.

Sample	Nominal (SRIM2008) implanted Al density (cm <sup>-3</sup> )	Implant temp. (°C)	Measured (SIMS) implanted Al density (cm <sup>-3</sup> )	Post implantation annealing	RT Hall hole density (cm <sup>-3</sup> )	RT resistivity (Ω cm)
305g <sup>2,3</sup>	$1.5 \times 10^{20}$	400	n. m.	MWA 2000 °C/30 s	$2 \times 10^{19}$	0.067
305b	$1.5 \times 10^{20}$	400	n. m.	CA 1950 °C/5 min	$7 \times 10^{18}$	0.097
294c <sup>2,3,7</sup>	$3 \times 10^{20}$	400	$2.94 \times 10^{20}$	MWA 2000 °C/30 s	$5 \times 10^{19}$	0.056
293a	$3 \times 10^{20}$	300	$2.94 \times 10^{20}$	MWA 2000 °C/30 s	$5 \times 10^{19}$	0.059
293e	$3 \times 10^{20}$	300	$2.94 \times 10^{20}$	CA 1950 °C/5 min	$5 \times 10^{19}$	0.052
296c	$5 \times 10^{20}$	300	$5.34 \times 10^{20}$	MWA 2000 °C/30 s	$3.5 \times 10^{20}$	0.023
296e	$5 \times 10^{20}$	300	$5.34 \times 10^{20}$	CA 1950 °C/5 min	$1.4 \times 10^{20}$	0.032

171 the samples of this study, such a correction resulted to  
 172 increase the resistivity experimental data of a few percent  
 173 (1%–4%); while more significant was the correction to the  
 174 Hall voltage, which led to Hall hole values of about  
 175 10%–30% lower than the rough experimental values,  
 176 depending on the contact pattern. It is worth noticing that  
 177 this clarification supports the electrical quality of the samples  
 178 here discussed, in fact, the correction guarantee that the  
 179 reached conductivity values are not apparently enhanced by  
 180 contact geometry. Four point vdP Hall measurements have  
 181 been performed at the temperature range of 30–680 K and  
 182 0.8–1 T variable magnetic field. In the samples of this study,  
 183 Hall hole densities from  $7 \times 10^{18} \text{ cm}^{-3}$  to  $1 \times 10^{21} \text{ cm}^{-3}$   
 184 have been obtained. The feasibility of the conversion of  
 185 “Hall hole density” into “drift hole density,” which is the  
 186 true value of free carriers, through the introduction of the  $r_H$   
 187 Hall factor will be critically discussed.

## 188 RESULTS AND DISCUSSION

189 Figures 1(a) and 1(b) compare the temperature dependence  
 190 of the Hall hole density and Hall hole mobility in two  
 191 samples with identical  $3 \times 10^{20} \text{ cm}^{-3}$  Al implanted concentration  
 192 and identical 2000 °C/30 s MWA but different implanta-  
 193 tion temperatures: 300 °C and 400 °C, samples 294c  
 194 and 293a of Table I, respectively. The curves of the two sam-  
 195 ples are identical within the experimental error. This result  
 196 allows us to assume that a 100 °C reduction of the implanta-  
 197 tion temperature, from 400 °C to 300 °C, does not affect the  
 198 quality of the subsequent post implantation annealing pro-  
 199 cess; therefore, it allows us to compare the results of the  
 200 transport measurements of all the samples of Table I, inde-  
 201 pendently of their implantation temperature.

202 Figures 2(a) and 2(b) depict the temperature dependen-  
 203 ces of the Hall hole density and Hall mobility for all the dif-  
 204 ferent implanted Al concentrations of the samples of Table I  
 205 and the different post implantation annealing: 1950 °C/5 min  
 206 CA (closed symbols) and 2000 °C/30 s MWA (open sym-  
 207 bols). For sake of precision, it can be added that Figs. 2(a)  
 208 and 2(b) contain all the samples of Table I except 294c. The  
 209 curves of Figs. 2(a) and 2(b) show that for identical  
 210 implanted Al doses, the MWA samples compared to their  
 211 CA counterparts show a generally higher carrier density and  
 212 a correspondingly lower mobility, while keeping very similar  
 213 trends of temperature dependence. The major physical differ-  
 214 ence between conventional and microwave heating may be  
 215 an interaction between the microwave field and the free car-  
 216 riers in the implanted layer, the more the electrical activation  
 217 of the implanted dopant proceeds. Such an effect could be  
 218 tested if identical CA and MWA thermal cycles could be  
 219 compared, but presently this is not possible because of the  
 220 technical constrains of the two annealing set-ups. In this sit-  
 221 uation, the differences between the correspondent CA and  
 222 MWA curves of Figs. 2(a) and 2(b) are ascribed to the 50 °C  
 223 higher temperature of the MWA compared to the CA.  
 224 Hereafter, the features of the curves of Figs. 2(a) and 2(b)  
 225 will be discussed only with respect to the value of the  
 226 implanted Al concentration.

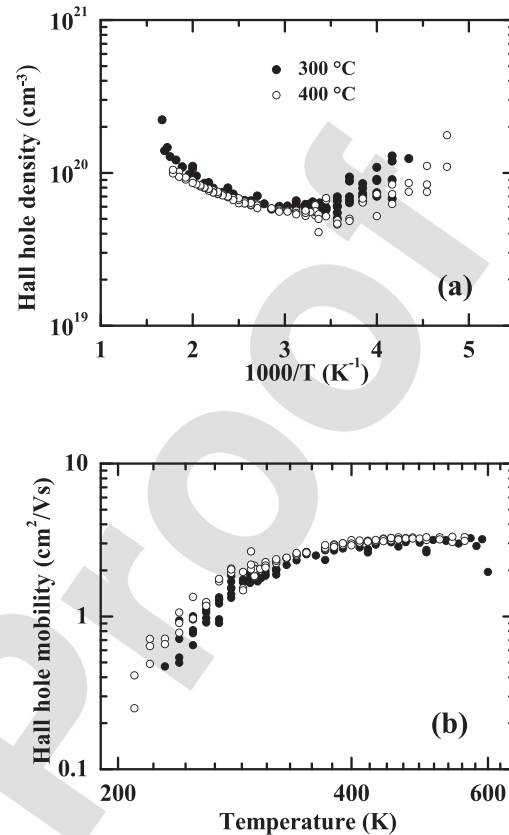


FIG. 1. Comparison of (a) the Hall hole density and (b) the Hall hole mobility for  $3 \times 10^{20} \text{ cm}^{-3}$  Al<sup>+</sup> implanted and 2000 °C/30 s MWA 4H-SiC samples, which are different only for the implantation temperature: (close symbols) 300 °C and (open symbols) 400 °C. The experimental data were corrected for contact size systematic error (see text).

Only the  $1.5 \times 10^{20} \text{ cm}^{-3}$  Al implanted specimens have  
 an Arrhenius plot of the Hall hole density data where an ex-  
 ponential trend is observable (see Fig. 2(a)), which is typical  
 for the carrier transport through valence band states in the  
 hole freeze-out regime. Such a trend takes place above about  
 200 K and it is consistent with an acceptor thermal ionization  
 energy of about 100 meV, in agreement with the conclusions  
 of Ref. 10. The temperature ( $T$ ) dependence of the corre-  
 spondent mobility curves (see Fig. 2(b)) shows a trend  
 almost equal to  $T^{-3/2}$  that is typical of phonon scattering.  
 This result says that the crystalline quality of these implanted  
 and annealed 4H-SiC specimens is preserved in spite of an  
 implanted Al concentration approaching the solubility value.  
 Notwithstanding this, a fitting of the Hall data was not per-  
 formed, because the model for transport discussed in Ref. 10  
 is reliable below an acceptor density of  $10^{20} \text{ cm}^{-3}$ . For tem-  
 peratures lower than 200 K, the data of this CA sample show  
 the hint of a minimum in the Hall density curve with the cor-  
 respondent mobility data decreasing more abruptly than the  
 typical trend expected for ionized impurity scattering, the  
 latter having a  $T^{3/2}$  temperature dependence or weaker.  
 These features are generally recognized as due to the onset  
 of a impurity band conduction, which prevails at low temper-  
 atures, whereas around the Hall density minimum a mixed  
 carrier transport takes place between IB and VB states, as  
 reviewed, e.g., by Mott in Ref. 18. The theoretical Hall den-  
 sity and mobility curves depicted in Ref. 10, however, show

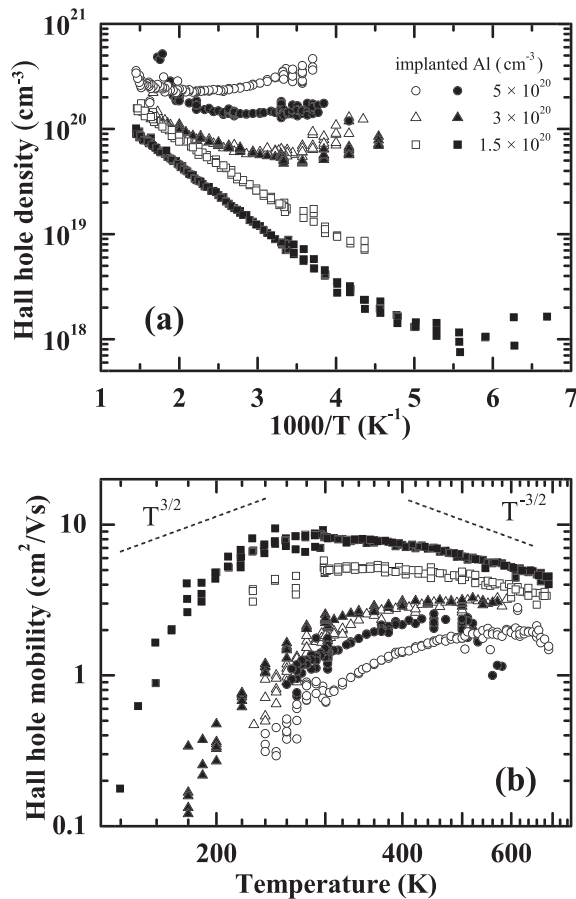


FIG. 2. Temperature dependence of: (a) the Hall hole density and (b) the Hall hole mobility of given Al implanted concentrations in  $8^\circ$  off-axis  $\langle 0001 \rangle$  high-purity semi-insulating 4H-SiC and different post implantation annealings: CA  $1950^\circ\text{C}/5$  min (full symbols), and MWA  $2000^\circ\text{C}/30$  s (open symbols). The implanted Al concentration is shown in the inset of (a). For comparison, the trends  $T^{3/2}$  and  $T^{-3/2}$  for ionized impurity scattering and non-polar phonon scattering, respectively, are shown as dashed lines in (b). The experimental data were corrected for contact size systematic error (see text).

a departure from experimental data towards the low temperatures, yet before such a minimum, suggesting that the influence of the transport through localized states is effective at higher temperatures in respect to that of such a minimum. In the  $1.1 \times 10^{20} \text{ cm}^{-3}$  Al implanted sample, in particular, a weak effect of the IB conduction can be presuable up to the proximity of RT.

The  $3 \times 10^{20} \text{ cm}^{-3}$  and  $5 \times 10^{20} \text{ cm}^{-3}$  Al implanted specimens show a weak temperature dependence of the Hall hole density values, weaker for higher implanted Al concentrations, and broad minima centred at about room temperature and above room temperature for the lower and higher implanted Al concentration, respectively (see Fig. 2(a)). The sign of the Hall coefficient was that expected for positive carriers at any temperature. The correspondent mobility values have a temperature dependence dominated by an almost flat trend at high temperature and a steep decrease with decreasing temperature, as for the  $1.5 \times 10^{20} \text{ cm}^{-3}$  Al implanted samples (see Fig. 2(b)). In the light of the global trends of all the samples, the occurrence of a mixed conduction where the transport through impurity states is relevant at any temperature has been hypothesized. The possibility to observe a significant IB

conduction at so high temperatures like room temperature and above is not usual and it is possible in p-type 4H-SiC, owing to the high thermal ionization energy of the Al acceptors. An IB conduction around room temperature has been previously reported in 4H-SiC for a much higher Al implanted concentration of  $1.5 \times 10^{21} \text{ cm}^{-3}$ , where the samples were implanted at comparable temperature than in the present study but annealed at a much lower temperature ( $1600^\circ\text{C}/10$  min).<sup>8</sup> Major differences between the results of this study and those of Ref. 8 are a higher hole density, higher mobility, and lower resistivity values in the former. These differences can be justified by a more efficient activation of the implanted dopant in this work, thanks to the higher annealing temperatures,  $1950^\circ\text{C}$ – $2000^\circ\text{C}$  against  $1600^\circ\text{C}$ . This result must be highlighted, because it indicates that these extreme annealing processes permit to reach a high enough acceptor density to induce a significant IB conduction around RT at lower implant dose in respect to Ref. 8, without detrimental effects on the mobility, which, on the contrary, is favoured probably by a lower amount of lattice disorder.

The estimation of the electrical activation (the fraction between dopant density in substitution positions and implanted dopant density) of a given post-implantation annealing process is generally possible if the transport of carriers takes place in the extended state band (VB), although the need of the Hall factor correction,  $r_H$ , which converts Hall into drift data, to avoid systematic inaccuracies, must be highlighted. In Ref. 10, it has been shown that this evaluation is reliable by fitting the data in the relaxation time approximation (RTA), till a maximum Al implanted concentration of  $1.12 \times 10^{20} \text{ cm}^{-3}$ , by adopting an empirically obtained Hall factor for Al doped p-type 4H-SiC.<sup>19</sup> In such p-type samples, the Hall factor must account for the occupancy of both the heavy and light hole valence bands and their anisotropy. In fact, in the case of two parallel channels “1” and “2,”  $r_H$  takes the form

$$r_H = (p_1 + p_2) e \frac{\sigma_1 \mu_{1H} + \sigma_2 \mu_{2H}}{(\sigma_1 + \sigma_2)^2}. \quad (1)$$

In Eq. (1),  $p_i$ ,  $\sigma_i$ , and  $\mu_{iH}$  are the hole density, the conductivity, and the Hall mobility in the  $i^{\text{th}}$  conduction channel ( $i = 1, 2$ );  $e$  is the electron charge. In the same channel of transport, the Hall and drift (true) mobility,  $\mu_{iH}$  and  $\mu_i$ , respectively, are generally different. The ratio  $\mu_{iH}/\mu_i$  is the intra-valley Hall factor,  $r_{Hi}$ , which for a transport into a band of extended states (i.e., the states of the valence or conduction band) can be computed in the frame of the RTA. In this framework,  $r_{Hi}$  is defined as the product of the scattering factor  $r_{Si} = \langle \tau_i^2 \rangle / \langle \tau_i \rangle^2$  with the mass anisotropy factor  $r_{Ai}$ , that is,  $r_{Hi} = r_{Si} r_{Ai}$  [Ref. 20 and references therein]. The scattering factor  $r_{Si}$  accounts for the kinetic energy distribution of free carriers within a given band (for non-monokinetic carriers), whereas the mass anisotropy factor  $r_{Ai}$  is a correction to  $r_{Si}$  due to a possible anisotropy of such a band. For p-type 4H-SiC, Eq. (1) has been used in Refs. 10 and 20–22, with some different assumptions, to describe the hole transport through the two parallel channels of the heavy and the light hole valence bands for acceptor concentration in the range  $2 \times 10^{15}$ – $1 \times 10^{20} \text{ cm}^{-3}$ .

331 When a transport through an impurity band is added in  
 332 parallel to the transport through extended states, which, in  
 333 this study, is the case for the  $3 \times 10^{20} \text{ cm}^{-3}$  and  
 334  $5 \times 10^{20} \text{ cm}^{-3}$  samples over the whole temperature range of  
 335 measurements, it is hard to apply Eq. (1) to obtain the Hall  
 336 factor. In fact, the interpretation of the Hall coefficient  $R_H$  as  
 337 a quantity simply related to the reverse of the carrier density  
 338 (*normal* Hall effect) becomes doubtful for an impurity band  
 339 conduction; the sign of the Hall voltage could even to be  
 340 inverted in this regime.<sup>18,23,24</sup> In this contest, the Hall factor  
 341  $r_H$  could empirically account for any deviation of the Hall  
 342 coefficient  $R_H$  from its *normal* meaning, but it could take  
 343 values not simply predictable. In any case, for the conduction  
 344 through localized states, the Hall factor  $r_H$  loses its usual  
 345 meaning because the hopping transport can be described  
 346 through a thermally activated hopping probability, which  
 347 cannot be calculated in terms of an energy dependent relaxa-  
 348 tion time. On the other hand, Mott suggested that in IB  
 349 conduction, around the transition to metal, if the Hall coefficient  
 350 does not have an abnormal sign, its value is not far from the  
 351 value expected for the carrier density.<sup>18</sup> However, the con-  
 352 version of the Hall values of Fig. 2(a) for the heaviest doped  
 353 samples in *drift* ones is not reliable and thus neither the cor-  
 354 respondent acceptor density can be simply estimated. In spite  
 355 of this conclusion, the following qualitative analysis on the  
 356 curves of Fig. 2(a) can be performed.

357 Although none of the curves of Fig. 2(a) shows carrier  
 358 exhaustion, the Hall hole density data of the samples with  
 359 the higher Al implanted concentration of  $5 \times 10^{20} \text{ cm}^{-3}$   
 360 could be used for a rough estimation of the maximum net  
 361 acceptor density (acceptor density minus compensating im-  
 362 purity density). In fact, the net acceptor density can be con-  
 363 sidered at least equal to the experimental Hall hole density  
 364 measured at higher temperature, where the transport through  
 365 extended states is expected to be dominant and then the  
 366 *intra-valley*  $r_H$  factor of Ref. 19 can be tentatively assumed  
 367 to correct the Hall data. The 2000 °C/30 s MWA sample  
 368 shows a maximum Hall density at the highest temperature of  
 369  $3.5 \times 10^{20} \text{ cm}^{-3}$ , which, if reduced of a  $r_H$  factor of about  
 370 0.6, is consistent with a net acceptor value of about  
 371  $2.2 \times 10^{20} \text{ cm}^{-3}$ . This density may correspond to a 100%  
 372 electrical activation for about a 50% compensation, or to a  
 373 more than 50% electrical activation for a 15% compensation.  
 374 The latter hypothesis seems to be more reasonable in the  
 375 light of the electrical activation and compensation which  
 376 have been obtained for Al implanted 4H-SiC samples in the  
 377 range  $5 \times 10^{19}$ – $1.5 \times 10^{20} \text{ cm}^{-3}$  and 1950 °C/5 min CA: 70%  
 378 and 10%–13%, respectively.<sup>10</sup>

379 A confirmation of the occurrence of a transport through  
 380 localized states can be inferred from the study of the temper-  
 381 ature dependence of the implanted material sheet resistance  
 382 or the material resistivity, which is the measured sheet resis-  
 383 tance multiplied by implanted layer thickness. No correction  
 384 to the implanted thickness needed to be accounted for Ref.  
 385 25, at any temperature, the surface/interface depletion of the  
 386 layer being negligible (however, such a correction would  
 387 have the effect to reduce further the resistivity data). Sheet  
 388 resistance has been measured in absence of magnetic field,  
 389 even if none magneto-resistance effect has ever been

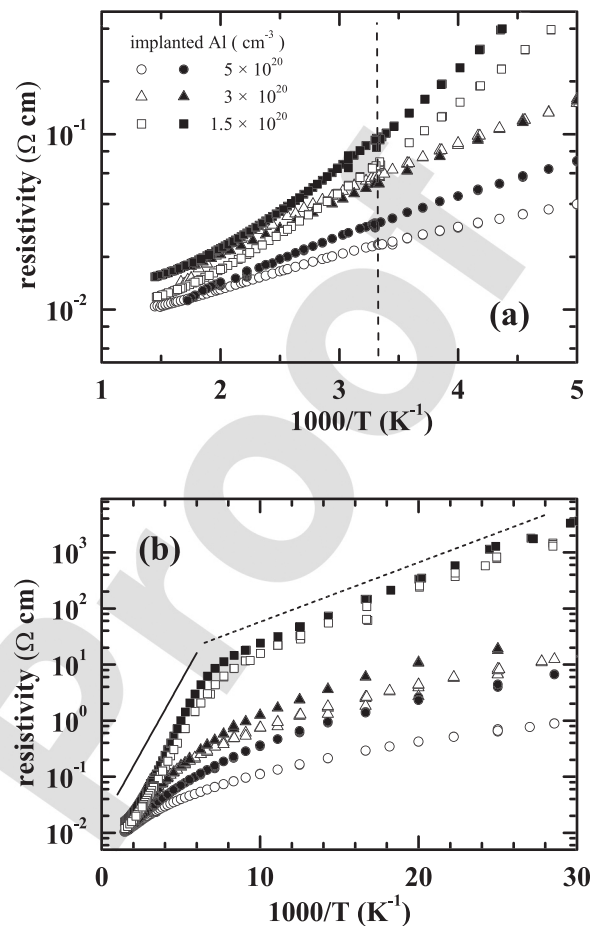


FIG. 3. Arrhenius plot of the resistivity data for all the sample of this study: (a) above and above RT, (b) over the whole range of temperature of measurements. The implanted Al concentrations are shown in the inset of (a). Open and full symbols refer to MWA and CA samples, respectively. The vertical dashed line of (a) corresponds to room temperature. Dashed and continuous lines in (b) show the exponential trends for 20 meV and 100 meV activation energies, respectively. The experimental data were corrected for contact size systematic error (see text).

detected for the samples of this study. Figs. 3(a) and 3(b) show the Arrhenius plots of the resistivity of all the samples of this study, the same data are plotted on two different temperature windows in order to clearly visualize the resistivity temperature dependence around and above RT in the case of Fig. 3(a), and even below RT in the case of Fig. 3(b). It is evident that, for each sample, sheet resistance measurements were performed until lower temperatures than those of Hall measurements, whose scattering increases more and more with the sample cooling. Such a scattering is due to the very low values of the Hall potential at such very high carrier densities, while the contacts preserve their ohmic behavior up to 10 K and the current can flow at any temperature through the implanted layers because the carrier density remains high thanks to the IB conduction. The sheet resistance, which increases with decreasing temperature, is measurable until the voltage drop at the vdP contacts does not overpasses the voltage limit of the used instrument set-up. The resistivity data, then obtained, show some general trends (see Figs. 3(a) and 3(b)), which confirm previously published results, see, as an example, Ref. 8. In particular, all the samples of this

study have resistivity values that decrease with increasing temperature as expected for a semiconductor material. This result is consistent with the published range of  $6.4 \times 10^{20}$ – $8.7 \times 10^{20} \text{ cm}^{-3}$  Al concentrations for the occurring of the metal to insulator transition (MIT), which has been observed in liquid phase epitaxial growth 4H-SiC materials.<sup>26</sup> In fact, in this study, the maximum value of Al implanted concentration is  $5 \times 10^{20} \text{ cm}^{-3}$ . It should also be noted that implanted materials are expected to contain more crystal disorders than the epitaxial ones. For elevated doping densities, the presence of crystal disorder could favor the persistence of a hopping conduction by inhibiting the MIT. Concerning the comparison of the two annealing methods, Figs. 3(a) and 3(b) show that for identical implanted Al concentration; the resistivity of the MWA specimen is generally lower than that of the CA one, which is attributed to a more efficient electrical activation by the MWA method because of its higher temperature. Finally, Figs. 3(a) and 3(b) show that the resistivity values decrease for increasing implanted Al concentration. The minimum RT resistivity obtained in the Al<sup>+</sup> 4H-SiC material of this study is  $2.3 \times 10^{-2} \Omega \text{ cm}$  for the  $5 \times 10^{20} \text{ cm}^{-3}$  implanted Al concentration and 2000 °C/30 s MWA. This result agrees with the conclusions of Heera *et al.*,<sup>27</sup> who calculated the values of minimum resistivity as a function of the acceptor density expected for hole transport through extended states in the ideal case of null compensation and predicted that resistivity data lower than such minimum values could be obtained only by achieving a transport through an impurity band. In particular, they<sup>27</sup> computed a resistivity of  $7 \times 10^{-2} \Omega \text{ cm}$  for hole transport in valence band with  $5 \times 10^{20} \text{ cm}^{-3}$  Al concentration.

The transition between a carrier conduction through band states to IB conduction is particularly evident in the  $1.5 \times 10^{20} \text{ cm}^{-3}$  Al implanted samples. In these samples, both the regimes are clearly visible in a wide temperature range, despite some mixed conduction effects in between. Around and above room temperature (see Fig. 3(a)), the Arrhenius plots of the p-type resistivity of these samples show a clear exponential trend with thermal activation energy of about 100 meV, which agrees with that obtained from the data of Fig. 2(a). By decreasing temperature (see the curves of Fig. 3(b)), the resistivity Arrhenius plots of the  $1.5 \times 10^{20} \text{ cm}^{-3}$  samples show a transition from the high temperature exponential trend to another exponential trend of much lower activation energy, about 20 meV, towards lower temperatures. This transition takes place in a narrow temperature window around about 200 K. Such a broken-straight line behavior can be commented according to the pioneering model of Miller and Abrahams.<sup>28</sup> This model describes the temperature dependence of the conductivity in semiconductor materials  $\sigma(T)$  as the sum of three thermally activated conduction mechanisms:  $\sigma_1$ ,  $\sigma_2$ , and  $\sigma_3$ , due to the transition into extended states (valence or conduction band), hopping to the higher impurity Hubbard band, and between impurity states, respectively

$$\begin{aligned} \sigma(T) &= \sigma_1 + \sigma_2 + \sigma_3 \\ &= \sigma_{01} e^{-\epsilon_1/K_B T} + \sigma_{02} e^{-\epsilon_2/K_B T} + \sigma_{03} e^{-\epsilon_3/K_B T}. \end{aligned} \quad (2)$$

In Eq. (2),  $\epsilon_1$ ,  $\epsilon_2$ , and  $\epsilon_3$  are the thermal activation of the three transport mechanisms, respectively, and  $K_B$  is the Boltzmann constant. Generally, the  $\sigma_1$  and  $\sigma_3$  contributions extend over wide temperature windows, while the possibility to detect the  $\sigma_2$  contribution is restricted to a narrow temperature range in between those of  $\sigma_1$  and  $\sigma_3$ , and limited to intermediate doping conditions even depending on the compensation ratio.<sup>29,30</sup> A linear trend appearing in the low temperature Arrhenius plot of the resistivity is, in the most of the cases, attributable to a transport through a hopping mechanism between an occupied dopant atom to a nearest unoccupied one. Therefore, in the case of the  $1.5 \times 10^{20} \text{ cm}^{-3}$  sample, the  $\approx 20$  meV activated transport was attributed to a hopping conduction between nearest Al acceptors. The model of this hopping mechanism predicts a thermal activation energy  $\epsilon_3$  dependent on compensation and doping level.<sup>28–31</sup>

A departure from the behavior of the  $1.5 \times 10^{20} \text{ cm}^{-3}$  sample is observed in the data of the heavier doped samples, of implanted Al concentration  $\geq 3 \times 10^{20} \text{ cm}^{-3}$ , whose resistivity Arrhenius plots do not evidence any reliable straight trend in the whole temperature range if accurately analyzed; therefore, in their low temperature conductivity data, neither the  $\sigma_2$  nor the  $\sigma_3$  contributions can be recognized. A similar behavior has been not claimed by Heera *et al.*,<sup>8</sup> who interpreted the resistivity data of all their samples, none of which displayed the maximum doping level here reached, in terms of the Miller and Abrahams model.

The ensemble of the results of this study on Al<sup>+</sup> implanted 4H-SiC materials, instead, agrees with the experimental results of Müller *et al.*<sup>32</sup> on Al doped 6H-SiC bulk materials. In fact, these authors performed temperature dependent Hall effect measurements on samples with specific resistivity in the range 1–8  $\Omega \text{ cm}$ . In all these samples, indications for impurity conduction at low temperatures have been found with the following major difference. In the lower doped samples ( $\rho > 0.2 \Omega \text{ cm}$ ), a sharp transition between impurity and valence band conduction transport was visible in the temperature dependence of specific resistivity, charge carrier concentration, and mobility. In highly doped samples ( $\rho < 0.2 \Omega \text{ cm}$ ), the same transition was no longer confined to a small temperature range and it was much less abrupt. Müller *et al.*<sup>32</sup> concluded that in their heavily Al doped bulk 6H-SiC, the impurity conduction was present at high temperatures so that at least two competing transport mechanisms took place simultaneously. In the Al<sup>+</sup> implanted 4H-SiC samples of this study, a resistivity one order of magnitude lower has been achieved and the phenomenon is much more evident.

The fact that no clear exponential trend can be recognized in our samples could be justified, at least partially, in terms of mixed conduction effects, involving extended and localized states. However, with the aim to confirm in our samples the departure from the nearly piecewise linear behavior predicted by Eq. (2) for the Arrhenius plot of the conductivity data, the  $\log_{10}[d\ln(\sigma)/d\ln(T)]$  function was numerically calculated from the conductivity of our samples, following the approach of, among others, Ref. 33. The slope  $p$  of the resulting data,

524 plotted as a function of  $\log_{10}[T]$ , is expected to equal the  
 525 value  $-1$  when the conductivity exhibits a thermally activated  
 526 behavior, like  $\sigma_0 e^{-\epsilon/K_B T}$ . Similarly, the sum of two (or more)  
 527 thermally activated behaviors, as they are in Eq. (2), must  
 528 lead to two (or more) linear traits with slope  $p = -1$ . This is  
 529 sketched in the inset of Fig. 4(a), which plots in double loga-  
 530 rithmic scale, the calculation of  $d\ln(\sigma_{teo})/d\ln(T)$  performed  
 531 on a test function  $\sigma_{teo} = \sigma_{01} e^{-\epsilon_1/K_B T} + \sigma_{03} e^{-\epsilon_3/K_B T}$ . The ex-  
 532 pectation of a  $p = -1$  slope is qualitatively fulfilled for the  
 533 low temperature data of the  $1.5 \times 10^{20} \text{ cm}^{-3}$  Al implanted  
 534 samples, as it appears in Fig. 4(a) for sample 305b of Table I,  
 535 for which the hypothesis of thermally activated hopping con-  
 536 duction between localized states at low temperature is con-  
 537 firmed. At the same time, Fig. 4(a) shows that the higher  
 538 temperature conductivity data of sample 305b, which should  
 539 correspond to valence band state transport, agree with a  $p$   
 540 value a little higher than unity. This is consistent with non-

exact linearity of the high temperature data in the Arrhenius 541  
 plot of Fig. 3(b), due to the effective temperature dependence 542  
 of the total VB density of the states and of the carrier mobility. 543  
 A transition region exists between these two different trans- 544  
 port regimes, indicated by an arrow in Fig. 4(a), consistent 545  
 with the trend of the theoretical example reported in the inset 546  
 of the same figure. Fig. 4(b) reports the result of the same type 547  
 of analysis of Fig. 4(a) but for one of the  $3 \times 10^{20} \text{ cm}^{-3}$  Al 548  
 implanted samples, more precisely sample 293e of Table I: 549  
 notwithstanding the scattering of the data; at low temperature, 550  
 their slope undoubtedly departs from the value  $p = -1$ , which, 551  
 however, seems to be a slope occurring just around RT. This 552  
 preliminary result roughly suggests the appearance of a trans- 553  
 port mechanism at lower temperatures different from the near- 554  
 est neighbor hopping, consistent with the Mott law 555  
 $\sigma = \sigma_0 e^{-\epsilon/K_B T^{0.25}}$ . A nearest neighbor hopping transport, 556  
 instead, could not be excluded around RT. The Mott law has 557  
 been derived in the treatment of the variable range hopping, 558  
 which is a transport mechanism effectively expected in prox- 559  
 imity of the MIT transition,<sup>31</sup> previously never pointed out in 560  
 p-type 4H-SiC. However, the given Mott law seems not to 561  
 fully explain the temperature dependence of all the heaviest 562  
 doped samples here discussed, although for all them, the de- 563  
 parture of the conductivity from Eq. (2) is confirmed. 564

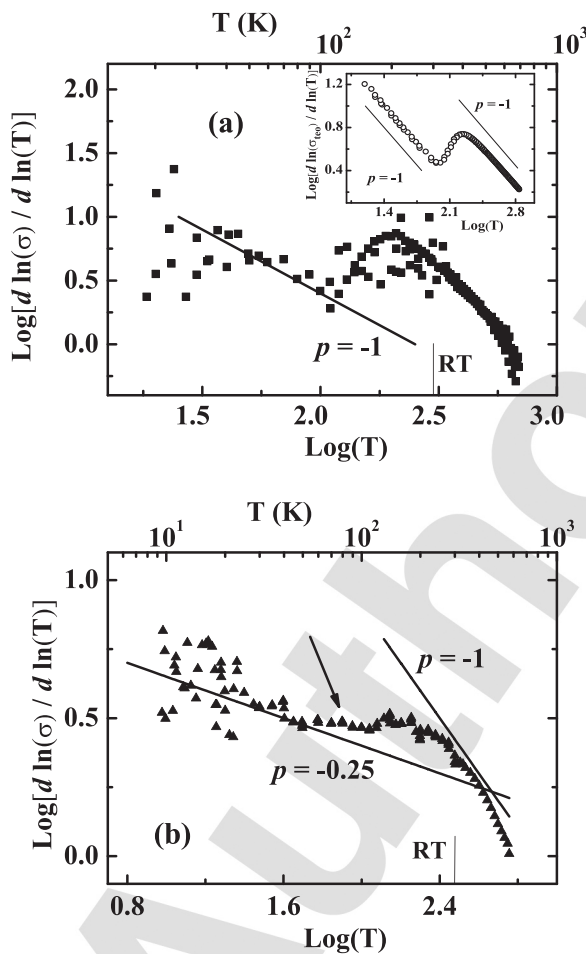


FIG. 4. Plot of  $\log_{10}[d\ln(\sigma)/d\ln(T)]$  versus  $\log_{10}[T]$  for the measured  $\sigma$  of  
 (a) sample 305b of Table I (Al implanted density of  $1.5 \times 10^{20} \text{ cm}^{-3}$ , CA  
 1950 °C/5 min; full square), (b) sample 293e of Table I (Al implanted  
 density of  $3 \times 10^{20} \text{ cm}^{-3}$ , CA 1950 °C/5 min; full triangle). Inset of Figure  
 (a):  $\log_{10}[d\ln(\sigma_{teo})/d\ln(T)]$  versus  $\log_{10}[T]$  for the test function  
 $\sigma_{teo} = 300 \exp(-0.1/K_B T) + 0.45 \exp(-0.021/K_B T)$ , which roughly ap-  
 proximate the conductivity data of the sample of Figure (a) like the sum of  
 two thermally activated contributions (see Eq. (2)). For guiding the eyes,  
 straight lines with slope either  $-1$  or  $-0.25$ , are also shown in the figures.  
 Moreover, for reference, a vertical thin line is placed at about RT and the  
 linear temperature scale is shown on the top axis, while arrows are drawn to  
 point the transition region between two different transport regimes.

## CONCLUSIONS

In conclusion, the unusual electrical properties of the  
 $\geq 3 \times 10^{20} \text{ cm}^{-3}$  Al implanted 4H-SiC samples that allow us  
 to observe an IB conduction over a large temperature win-  
 dow just around RT associated to a low p-type 4H-SiC mate-  
 rial resistivity is possible thanks to the simultaneous  
 occurrence of three aspects

- (1) An implanted dopant concentration above the Al solubil-  
 ity limit of  $2 \times 10^{20} \text{ cm}^{-2}$ .
- (2) A very efficient electrical activation process due to the  
 extremely high post implantation annealing temperatures  
 of 1950 °C and 2000 °C.
- (3) The high thermal ionization energy of the acceptors in p-  
 type 4H-SiC.

A nearly temperature independent free hole density  
 can be obtained around RT in these samples, a feature that  
 can guarantee good thermal stability in applications where  
 such a stability is required. Ion implantation even permits  
 to simplify the processing steps for reaching such a condi-  
 tion in selected areas. Weakly  $T$ -dependent transport prop-  
 erties were obtained, in this work, at lower implant dose  
 and higher electrical activation of the implanted impurities  
 in respect to results of other authors. No significant effects  
 due to the implant temperature variation between 300 °C  
 and 400 °C were evidenced. In  $5 \times 10^{20} \text{ cm}^{-3}$  Al implanted  
 samples, hole density values overcoming the Al solubility  
 limit in 4H-SiC were reached, consistent with at least a  
 50% electrical activation if a 15% compensation is sup-  
 posed. These doping conditions lead to the lowest RT resis-  
 tivity values ever reported in the literature for p-type 4H-  
 SiC, to the best of the authors knowledge, with more  
 favourable results in MWA samples, owing to the 50 °C

597 higher temperature of the treatment in respect to CA. The  
598 temperature dependence of the resistivity was well  
599 explained by the model of Miller and Abrahams in the  
600 samples of carrier density lower than  $3 \times 10^{20}$  (here inves-  
601 tigated and from the literature), whereas a deviation from  
602 this behaviour is observed above such a density, consistent  
603 with the occurrence of a variable range hopping transport  
604 mechanism at low temperatures.

605 Theory and experiments on impurity band conduction  
606 lead to conclude that such a transport mechanism takes place  
607 at higher and higher temperature with the increasing of the  
608 dopant ionization energy. SiC is certainly a good material to  
609 see this trend because of the quite deep energy level of every  
610 dopant species. Actually, SiC was the first semiconductor  
611 where transport through an impurity band was hypothesized  
612 in 1946.<sup>34</sup> The novelty to see an impurity band transport  
613 around room temperature in p-type SiC dates on the years  
614 2004–2006, roughly.<sup>8,9,32</sup> The novelty to obtain an impurity  
615 band transport with features of interest for practical devices  
616 is shown in the present study.

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